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# Pixyz Documentation

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## Package Reference

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Pixyz is a library for developing deep generative models in a more concise, intuitive and extendable way!



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pixyz.distributions (Distribution API)

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## 1.1 Distribution

```
class pixyz.distributions.distributions.Distribution(var, cond_var=[], name='p',  
                                                features_shape=torch.Size([]),  
                                                atomic=True)
```

Bases: torch.nn.modules.module.Module

Distribution class. In Pixyz, all distributions are required to inherit this class.

### Examples

```
>>> import torch
>>> from torch.nn import functional as F
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...            features_shape=[64], name="p1")
>>> print(p1)
Distribution:
  p_{1}(x)
Network architecture:
  Normal(
    name=p_{1}, distribution_name=Normal,
    var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([64])
    (loc): torch.Size([1, 64])
    (scale): torch.Size([1, 64])
  )
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...            features_shape=[64], name="p2")
>>> print(p2)
```

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```
Distribution:
  p_{2}(x|y)
Network architecture:
  Normal(
    name=p_{2}, distribution_name=Normal,
    var=['x'], cond_var=['y'], input_var=['y'], features_shape=torch.Size([64])
    (scale): torch.Size([1, 64])
  )
```

```
>>> # Conditional distribution (by neural networks)
>>> class P(Normal):
...     def __init__(self):
...         super().__init__(var=["x"], cond_var=["y"], name="p3")
...         self.model_loc = nn.Linear(128, 64)
...         self.model_scale = nn.Linear(128, 64)
...     def forward(self, y):
...         return {"loc": self.model_loc(y), "scale": F.softplus(self.model_
↪scale(y))}
>>> p3 = P()
>>> print(p3)
Distribution:
  p_{3}(x|y)
Network architecture:
  P(
    name=p_{3}, distribution_name=Normal,
    var=['x'], cond_var=['y'], input_var=['y'], features_shape=torch.Size([])
    (model_loc): Linear(in_features=128, out_features=64, bias=True)
    (model_scale): Linear(in_features=128, out_features=64, bias=True)
  )
```

```
__init__(var, cond_var=[], name='p', features_shape=torch.Size([]), atomic=True)
```

### Parameters

- **var** (list of str) – Variables of this distribution.
- **cond\_var** (list of str, defaults to []) – Conditional variables of this distribution. In case that cond\_var is not empty, we must set the corresponding inputs to sample variables.
- **name** (str, defaults to “p”) – Name of this distribution. This name is displayed in *prob\_text* and *prob\_factorized\_text*.
- **features\_shape** (torch.Size or list, defaults to torch.Size()) – Shape of dimensions (features) of this distribution.

### graph

#### distribution\_name

Name of this distribution class.

**Type** str

#### name

Name of this distribution displayed in *prob\_text* and *prob\_factorized\_text*.

**Type** str

#### var

Variables of this distribution.

**Type** list



**cond\_var**

Conditional variables of this distribution.

**Type** list

**input\_var**

Input variables of this distribution. Normally, it has same values as `cond_var`.

**Type** list

**prob\_text**

Return a formula of the (joint) probability distribution.

**Type** str

**prob\_factorized\_text**

Return a formula of the factorized probability distribution.

**Type** str

**prob\_joint\_factorized\_and\_text**

Return a formula of the factorized and the (joint) probability distributions.

**Type** str

**features\_shape**

Shape of features of this distribution.

**Type** torch.Size or list

**sample** (*x\_dict*={}, *batch\_n*=None, *sample\_shape*=torch.Size([]), *return\_all*=True, *reparam*=False)

Sample variables of this distribution. If `cond_var` is not empty, you should set inputs as dict.

**Parameters**

- **x\_dict** (torch.Tensor, list, or dict, defaults to {}) – Input variables.
- **batch\_n** (int, defaults to None.) – Set batch size of parameters.
- **sample\_shape** (list or NoneType, defaults to torch.Size()) – Shape of generating samples.
- **return\_all** (bool, defaults to True) – Choose whether the output contains input variables.
- **reparam** (bool, defaults to False.) – Choose whether we sample variables with re-parameterized trick.

**Returns** **output** – Samples of this distribution.

**Return type** dict

**Examples**

```
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10, 2])
>>> print(p)
Distribution:
  p(x)
Network architecture:
  Normal(
```

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```

        name=p, distribution_name=Normal,
        var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([10, 2])
        (loc): torch.Size([1, 10, 2])
        (scale): torch.Size([1, 10, 2])
    )
>>> p.sample()["x"].shape # (batch_n=1, features_shape)
torch.Size([1, 10, 2])
>>> p.sample(batch_n=20)["x"].shape # (batch_n, features_shape)
torch.Size([20, 10, 2])
>>> p.sample(batch_n=20, sample_shape=[40, 30])["x"].shape # (sample_shape,
↳batch_n, features_shape)
torch.Size([40, 30, 20, 10, 2])

```

```

>>> # Conditional distribution
>>> p = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...           features_shape=[10])
>>> print(p)
Distribution:
  p(x|y)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=['y'], input_var=['y'], features_shape=torch.
↳Size([10])
    (scale): torch.Size([1, 10])
  )
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> sample_a = torch.randn(1, 10) # Psuedo data
>>> sample = p.sample({"y": sample_y})
>>> print(sample) # input_var + var # doctest: +SKIP
{'y': tensor([[ -0.5182,  0.3484,  0.9042,  0.1914,  0.6905,
                -1.0859, -0.4433, -0.0255,  0.8198,  0.4571]]),
 'x': tensor([[ -0.7205, -1.3996,  0.5528, -0.3059,  0.5384,
                -1.4976, -0.1480,  0.0841, 0.3321,  0.5561]])}
>>> sample = p.sample({"y": sample_y, "a": sample_a}) # Redundant input ("a")
>>> print(sample) # input_var + var + "a" (redundant input) # doctest: +SKIP
{'y': tensor([[ 1.3582, -1.1151, -0.8111,  1.0630,  1.1633,
                0.3855,  2.6324, -0.9357, -0.8649, -0.6015]]),
 'a': tensor([[ -0.1874,  1.7958, -1.4084, -2.5646,  1.0868,
                -0.7523, -0.0852, -2.4222, -0.3914, -0.9755]]),
 'x': tensor([[ -0.3272, -0.5222, -1.3659,  1.8386,  2.3204,
                0.3686,  0.6311, -1.1208, 0.3656, -0.6683]])}

```

**has\_reparam****sample\_mean** (*x\_dict*={})

Return the mean of the distribution.

**Parameters** *x\_dict* (dict, defaults to {}) – Parameters of this distribution.**Examples**

```

>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution

```

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```

>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> mean = p1.sample_mean()
>>> print(mean)
tensor([[0., 0., 0., 0., 0., 0., 0., 0., 0., 0.]])

>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...            features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> mean = p2.sample_mean({"y": sample_y})
>>> print(mean) # doctest: +SKIP
tensor([[ -0.2189, -1.0310, -0.1917, -0.3085,  1.5190, -0.9037,  1.2559,  0.
  ↪1410,
          1.2810, -0.6681]])

```

**sample\_variance** (*x\_dict*={})

Return the variance of the distribution.

**Parameters** **x\_dict** (dict, defaults to {}) – Parameters of this distribution.

### Examples

```

>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...            features_shape=[10], name="p1")
>>> var = p1.sample_variance()
>>> print(var)
tensor([[1., 1., 1., 1., 1., 1., 1., 1., 1., 1.]])

>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...            features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> var = p2.sample_variance({"y": sample_y})
>>> print(var) # doctest: +SKIP
tensor([[1., 1., 1., 1., 1., 1., 1., 1., 1., 1.]])

```

**get\_log\_prob** (*x\_dict*, *sum\_features*=True, *feature\_dims*=None)

Giving variables, this method returns values of log-pdf.

#### Parameters

- **x\_dict** (*dict*) – Input variables.
- **sum\_features** (bool, defaults to True) – Whether the output is summed across some dimensions which are specified by *feature\_dims*.
- **feature\_dims** (list or NoneType, defaults to None) – Set dimensions to sum across the output.

**Returns** **log\_prob** – Values of log-probability density/mass function.**Return type** torch.Tensor

## Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> log_prob = p1.log_prob({"x": sample_x})
>>> print(log_prob) # doctest: +SKIP
tensor([-16.1153])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> log_prob = p2.log_prob({"x": sample_x, "y": sample_y})
>>> print(log_prob) # doctest: +SKIP
tensor([-21.5251])
```

**get\_entropy** (*x\_dict*={}, *sum\_features*=True, *feature\_dims*=None)

Giving variables, this method returns values of entropy.

### Parameters

- **x\_dict** (*dict*, defaults to {}) – Input variables.
- **sum\_features** (*bool*, defaults to True) – Whether the output is summed across some dimensions which are specified by *feature\_dims*.
- **feature\_dims** (*list* or *NoneType*, defaults to None) – Set dimensions to sum across the output.

**Returns** **entropy** – Values of entropy.

**Return type** torch.Tensor

## Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> entropy = p1.get_entropy()
>>> print(entropy)
tensor([14.1894])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> entropy = p2.get_entropy({"y": sample_y})
>>> print(entropy)
tensor([14.1894])
```

**log\_prob** (*sum\_features*=True, *feature\_dims*=None)

Return an instance of *pixyz.losses.LogProb*.

**Parameters**

- **sum\_features** (bool, defaults to True) – Whether the output is summed across some axes (dimensions) which are specified by `feature_dims`.
- **feature\_dims** (list or NoneType, defaults to None) – Set axes to sum across the output.

**Returns** An instance of `pixyz.losses.LogProb`

**Return type** `pixyz.losses.LogProb`

**Examples**

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> log_prob = p1.log_prob().eval({"x": sample_x})
>>> print(log_prob) # doctest: +SKIP
tensor([-16.1153])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> log_prob = p2.log_prob().eval({"x": sample_x, "y": sample_y})
>>> print(log_prob) # doctest: +SKIP
tensor([-21.5251])
```

**prob** (`sum_features=True, feature_dims=None`)

Return an instance of `pixyz.losses.Prob`.

**Parameters**

- **sum\_features** (bool, defaults to True) – Choose whether the output is summed across some axes (dimensions) which are specified by `feature_dims`.
- **feature\_dims** (list or NoneType, defaults to None) – Set dimensions to sum across the output. (Note: this parameter is not used for now.)

**Returns** An instance of `pixyz.losses.Prob`

**Return type** `pixyz.losses.Prob`

**Examples**

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> prob = p1.prob().eval({"x": sample_x})
>>> print(prob) # doctest: +SKIP
tensor([4.0933e-07])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> prob = p2.prob().eval({"x": sample_x, "y": sample_y})
>>> print(prob) # doctest: +SKIP
tensor([2.9628e-09])
```

**forward** (\*args, \*\*kwargs)

When this class is inherited by DNNs, this method should be overridden.

**replace\_var** (\*\*replace\_dict)

Return an instance of `pixyz.distributions.ReplaceVarDistribution`.

**Parameters** **replace\_dict** (dict) – Dictionary.

**Returns** An instance of `pixyz.distributions.ReplaceVarDistribution`

**Return type** `pixyz.distributions.ReplaceVarDistribution`

**marginalize\_var** (marginalize\_list)

Return an instance of `pixyz.distributions.MarginalizeVarDistribution`.

**Parameters** **marginalize\_list** (list or other) – Variables to marginalize.

**Returns** An instance of `pixyz.distributions.MarginalizeVarDistribution`

**Return type** `pixyz.distributions.MarginalizeVarDistribution`

**extra\_repr** ()

Set the extra representation of the module

To print customized extra information, you should re-implement this method in your own modules. Both single-line and multi-line strings are acceptable.

## 1.2 Exponential families

### 1.2.1 Normal

**class** `pixyz.distributions.Normal` (var=['x'], cond\_var=[], name='p', features\_shape=torch.Size([]), loc=None, scale=None)

Bases: `pixyz.distributions.distributions.DistributionBase`

Normal distribution parameterized by loc and scale.

**params\_keys**

Return the list of parameter names for this distribution.

**Type** list

**distribution\_torch\_class**

Return the class of PyTorch distribution.

**distribution\_name**

Name of this distribution class.

**Type** str

**has\_reparam**

### 1.2.2 Laplace

```
class pixyz.distributions.Laplace (var=['x'],      cond_var=[],      name='p',      fea-
                                tures_shape=torch.Size([]), loc=None, scale=None)
    Bases: pixyz.distributions.distributions.DistributionBase
    Laplace distribution parameterized by loc and scale.

    params_keys
        Return the list of parameter names for this distribution.

        Type list

    distribution_torch_class
        Return the class of PyTorch distribution.

    distribution_name
        Name of this distribution class.

        Type str

    has_reparam
```

### 1.2.3 Bernoulli

```
class pixyz.distributions.Bernoulli (var=['x'],      cond_var=[],      name='p',      fea-
                                tures_shape=torch.Size([]), probs=None)
    Bases: pixyz.distributions.distributions.DistributionBase
    Bernoulli distribution parameterized by probs.

    params_keys
        Return the list of parameter names for this distribution.

        Type list

    distribution_torch_class
        Return the class of PyTorch distribution.

    distribution_name
        Name of this distribution class.

        Type str

    has_reparam
```

### 1.2.4 RelaxedBernoulli

```
class pixyz.distributions.RelaxedBernoulli (var=['x'],  cond_var=[],  name='p',  fea-
                                tures_shape=torch.Size([]),      tempera-
                                ture=tensor(0.1000), probs=None)
    Bases: pixyz.distributions.exponential_distributions.Bernoulli
    Relaxed (re-parameterizable) Bernoulli distribution parameterized by probs and temperature.

    params_keys
        Return the list of parameter names for this distribution.

        Type list

    distribution_torch_class
        Use relaxed version only when sampling
```

**distribution\_name**

Name of this distribution class.

**Type** str

**set\_dist** (*x\_dict*={}, *batch\_n*=None, *sampling*=False, *\*\*kwargs*)

Set dist as PyTorch distributions given parameters.

This requires that *params\_keys* and *distribution\_torch\_class* are set.

**Parameters**

- **x\_dict** (dict, defaults to {}) – Parameters of this distribution.
- **batch\_n** (int, defaults to None.) – Set batch size of parameters.
- **sampling** (bool defaults to False.) – If it is false, the distribution will not be relaxed to compute log\_prob.
- **\*\*kwargs** – Arbitrary keyword arguments.

**sample** (*x\_dict*={}, *batch\_n*=None, *sample\_shape*=torch.Size([]), *return\_all*=True, *reparam*=False)

Sample variables of this distribution. If *cond\_var* is not empty, you should set inputs as dict.

**Parameters**

- **x\_dict** (torch.Tensor, list, or dict, defaults to {}) – Input variables.
- **batch\_n** (int, defaults to None.) – Set batch size of parameters.
- **sample\_shape** (list or NoneType, defaults to torch.Size()) – Shape of generating samples.
- **return\_all** (bool, defaults to True) – Choose whether the output contains input variables.
- **reparam** (bool, defaults to False.) – Choose whether we sample variables with reparameterized trick.

**Returns** output – Samples of this distribution.

**Return type** dict

**Examples**

```
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10, 2])
>>> print(p)
Distribution:
p(x)
Network architecture:
Normal(
  name=p, distribution_name=Normal,
  var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([10, 2])
  (loc): torch.Size([1, 10, 2])
  (scale): torch.Size([1, 10, 2])
)
>>> p.sample()["x"].shape # (batch_n=1, features_shape)
torch.Size([1, 10, 2])
>>> p.sample(batch_n=20)["x"].shape # (batch_n, features_shape)
```

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```
torch.Size([20, 10, 2])
>>> p.sample(batch_n=20, sample_shape=[40, 30])["x"].shape # (sample_shape, ↵
↵batch_n, features_shape)
torch.Size([40, 30, 20, 10, 2])
```

```
>>> # Conditional distribution
>>> p = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...           features_shape=[10])
>>> print(p)
Distribution:
  p(x|y)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=['y'], input_var=['y'], features_shape=torch.
↵Size([10])
    (scale): torch.Size([1, 10])
  )
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> sample_a = torch.randn(1, 10) # Psuedo data
>>> sample = p.sample({"y": sample_y})
>>> print(sample) # input_var + var # doctest: +SKIP
{'y': tensor([[ -0.5182,  0.3484,  0.9042,  0.1914,  0.6905,
                -1.0859, -0.4433, -0.0255,  0.8198,  0.4571]]),
 'x': tensor([[ -0.7205, -1.3996,  0.5528, -0.3059,  0.5384,
                -1.4976, -0.1480,  0.0841, 0.3321,  0.5561]])}
>>> sample = p.sample({"y": sample_y, "a": sample_a}) # Redundant input ("a")
>>> print(sample) # input_var + var + "a" (redundant input) # doctest: +SKIP
{'y': tensor([[ 1.3582, -1.1151, -0.8111,  1.0630,  1.1633,
                0.3855,  2.6324, -0.9357, -0.8649, -0.6015]]),
 'a': tensor([[ -0.1874,  1.7958, -1.4084, -2.5646,  1.0868,
                -0.7523, -0.0852, -2.4222, -0.3914, -0.9755]]),
 'x': tensor([[ -0.3272, -0.5222, -1.3659,  1.8386,  2.3204,
                0.3686,  0.6311, -1.1208, 0.3656, -0.6683]])}
```

**has\_reparam**

## 1.2.5 FactorizedBernoulli

```
class pixyz.distributions.FactorizedBernoulli(var=['x'], cond_var=[], name='p',
                                              features_shape=torch.Size([]),
                                              probs=None)
```

Bases: pixyz.distributions.exponential\_distributions.Bernoulli

Factorized Bernoulli distribution parameterized by probs.

### References

[Vedantam+ 2017] Generative Models of Visually Grounded Imagination

**distribution\_name**

Name of this distribution class.

**Type** str

**get\_log\_prob** (*x\_dict*)

Giving variables, this method returns values of log-pdf.

**Parameters**

- **x\_dict** (*dict*) – Input variables.
- **sum\_features** (*bool*, defaults to *True*) – Whether the output is summed across some dimensions which are specified by *feature\_dims*.
- **feature\_dims** (*list* or *NoneType*, defaults to *None*) – Set dimensions to sum across the output.

**Returns** **log\_prob** – Values of log-probability density/mass function.

**Return type** `torch.Tensor`

**Examples**

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> log_prob = p1.log_prob({"x": sample_x})
>>> print(log_prob) # doctest: +SKIP
tensor([-16.1153])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> log_prob = p2.log_prob({"x": sample_x, "y": sample_y})
>>> print(log_prob) # doctest: +SKIP
tensor([-21.5251])
```

## 1.2.6 Categorical

**class** `pixyz.distributions.Categorical` (*var=['x']*, *cond\_var=[]*, *name='p'*, *features\_shape=torch.Size([])*, *probs=None*)

Bases: `pixyz.distributions.distributions.DistributionBase`

Categorical distribution parameterized by *probs*.

**params\_keys**

Return the list of parameter names for this distribution.

**Type** `list`

**distribution\_torch\_class**

Return the class of PyTorch distribution.

**distribution\_name**

Name of this distribution class.

**Type** `str`

**has\_reparam**

## 1.2.7 RelaxedCategorical

```
class pixyz.distributions.RelaxedCategorical (var=['x'], cond_var=[], name='p',
                                             features_shape=torch.Size([]), tempera-
                                             ture=tensor(0.1000), probs=None)
```

Bases: `pixyz.distributions.exponential_distributions.Categorical`

Relaxed (re-parameterizable) categorical distribution parameterized by probs and temperature. Notes: a shape of temperature should contain the event shape of this Categorical distribution.

### **params\_keys**

Return the list of parameter names for this distribution.

**Type** list

### **distribution\_torch\_class**

Use relaxed version only when sampling

### **distribution\_name**

Name of this distribution class.

**Type** str

**set\_dict** (*x\_dict*={}, *batch\_n*=None, *sampling*=False, *\*\*kwargs*)

Set dict as PyTorch distributions given parameters.

This requires that `params_keys` and `distribution_torch_class` are set.

### **Parameters**

- **x\_dict** (dict, defaults to {}) – Parameters of this distribution.
- **batch\_n** (int, defaults to None.) – Set batch size of parameters.
- **sampling** (bool defaults to False.) – If it is false, the distribution will not be relaxed to compute log\_prob.
- **\*\*kwargs** – Arbitrary keyword arguments.

**sample** (*x\_dict*={}, *batch\_n*=None, *sample\_shape*=torch.Size([]), *return\_all*=True, *reparam*=False)

Sample variables of this distribution. If `cond_var` is not empty, you should set inputs as dict.

### **Parameters**

- **x\_dict** (torch.Tensor, list, or dict, defaults to {}) – Input variables.
- **batch\_n** (int, defaults to None.) – Set batch size of parameters.
- **sample\_shape** (list or NoneType, defaults to torch.Size()) – Shape of generating samples.
- **return\_all** (bool, defaults to True) – Choose whether the output contains input variables.
- **reparam** (bool, defaults to False.) – Choose whether we sample variables with re-parameterized trick.

**Returns output** – Samples of this distribution.

**Return type** dict

## Examples

```
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10, 2])
>>> print(p)
Distribution:
  p(x)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([10, 2])
    (loc): torch.Size([1, 10, 2])
    (scale): torch.Size([1, 10, 2])
  )
>>> p.sample()["x"].shape # (batch_n=1, features_shape)
torch.Size([1, 10, 2])
>>> p.sample(batch_n=20)["x"].shape # (batch_n, features_shape)
torch.Size([20, 10, 2])
>>> p.sample(batch_n=20, sample_shape=[40, 30])["x"].shape # (sample_shape,
↳ batch_n, features_shape)
torch.Size([40, 30, 20, 10, 2])
```

```
>>> # Conditional distribution
>>> p = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...           features_shape=[10])
>>> print(p)
Distribution:
  p(x|y)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=['y'], input_var=['y'], features_shape=torch.
↳ Size([10])
    (scale): torch.Size([1, 10])
  )
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> sample_a = torch.randn(1, 10) # Psuedo data
>>> sample = p.sample({"y": sample_y})
>>> print(sample) # input_var + var # doctest: +SKIP
{'y': tensor([[ -0.5182,  0.3484,  0.9042,  0.1914,  0.6905,
                -1.0859, -0.4433, -0.0255,  0.8198,  0.4571]]),
 'x': tensor([[ -0.7205, -1.3996,  0.5528, -0.3059,  0.5384,
                -1.4976, -0.1480,  0.0841, 0.3321,  0.5561]])}
>>> sample = p.sample({"y": sample_y, "a": sample_a}) # Redundant input ("a")
>>> print(sample) # input_var + var + "a" (redundant input) # doctest: +SKIP
{'y': tensor([[ 1.3582, -1.1151, -0.8111,  1.0630,  1.1633,
                0.3855,  2.6324, -0.9357, -0.8649, -0.6015]]),
 'a': tensor([[ -0.1874,  1.7958, -1.4084, -2.5646,  1.0868,
                -0.7523, -0.0852, -2.4222, -0.3914, -0.9755]]),
 'x': tensor([[ -0.3272, -0.5222, -1.3659,  1.8386,  2.3204,
                0.3686,  0.6311, -1.1208, 0.3656, -0.6683]])}
```

**has\_reparam**

### 1.2.8 Beta

```
class pixyz.distributions.Beta (var=['x'],      cond_var=[],      name='p',      fea-
                                tures_shape=torch.Size([]),  concentration1=None,  concen-
                                tration0=None)
```

Bases: pixyz.distributions.distributions.DistributionBase

Beta distribution parameterized by concentration1 and concentration0.

**params\_keys**

Return the list of parameter names for this distribution.

**Type** list

**distribution\_torch\_class**

Return the class of PyTorch distribution.

**distribution\_name**

Name of this distribution class.

**Type** str

**has\_reparam**

### 1.2.9 Dirichlet

```
class pixyz.distributions.Dirichlet (var=['x'],      cond_var=[],      name='p',      fea-
                                tures_shape=torch.Size([]),  concentration=None)
```

Bases: pixyz.distributions.distributions.DistributionBase

Dirichlet distribution parameterized by concentration.

**params\_keys**

Return the list of parameter names for this distribution.

**Type** list

**distribution\_torch\_class**

Return the class of PyTorch distribution.

**distribution\_name**

Name of this distribution class.

**Type** str

**has\_reparam**

### 1.2.10 Gamma

```
class pixyz.distributions.Gamma (var=['x'],      cond_var=[],      name='p',      fea-
                                tures_shape=torch.Size([]),  concentration=None,  rate=None)
```

Bases: pixyz.distributions.distributions.DistributionBase

Gamma distribution parameterized by concentration and rate.

**params\_keys**

Return the list of parameter names for this distribution.

**Type** list

**distribution\_torch\_class**

Return the class of PyTorch distribution.

**distribution\_name**

Name of this distribution class.

**Type** str**has\_reparam**

## 1.3 Complex distributions

### 1.3.1 MixtureModel

**class** pixyz.distributions.**MixtureModel** (*distributions, prior, name='p'*)Bases: *pixyz.distributions.distributions.Distribution*

Mixture models.

$$p(x) = \sum_i p(x|z=i)p(z=i)$$

#### Examples

```

>>> from pixyz.distributions import Normal, Categorical
>>> from pixyz.distributions.mixture_distributions import MixtureModel
>>> z_dim = 3 # the number of mixture
>>> x_dim = 2 # the input dimension.
>>> distributions = [] # the list of distributions
>>> for i in range(z_dim):
...     loc = torch.randn(x_dim) # initialize the value of location (mean)
...     scale = torch.empty(x_dim).fill_(1.) # initialize the value of scale
...     distributions.append(Normal(loc=loc, scale=scale, var=["x"], name="p_%d"
...     ↪ %i))
>>> probs = torch.empty(z_dim).fill_(1. / z_dim) # initialize the value of
...     ↪ probabilities
>>> prior = Categorical(probs=probs, var=["z"], name="prior")
>>> p = MixtureModel(distributions=distributions, prior=prior)
>>> print(p)
Distribution:
  p(x) = p_{0}(x|z=0)prior(z=0) + p_{1}(x|z=1)prior(z=1) + p_{2}(x|z=2)prior(z=2)
Network architecture:
  MixtureModel(
    name=p, distribution_name=Mixture Model,
    var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([2])
    (distributions): ModuleList(
      (0): Normal(
        name=p_{0}, distribution_name=Normal,
        var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([2])
        (loc): torch.Size([1, 2])
        (scale): torch.Size([1, 2])
      )
      (1): Normal(
        name=p_{1}, distribution_name=Normal,
        var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([2])
        (loc): torch.Size([1, 2])
        (scale): torch.Size([1, 2])
      )
    )
  )

```

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```

    )
    (2): Normal(
      name=p_{2}, distribution_name=Normal,
      var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([2])
      (loc): torch.Size([1, 2])
      (scale): torch.Size([1, 2])
    )
  )
  (prior): Categorical(
    name=prior, distribution_name=Categorical,
    var=['z'], cond_var=[], input_var=[], features_shape=torch.Size([3])
    (probs): torch.Size([1, 3])
  )
)

```

**\_\_init\_\_** (*distributions, prior, name='p'*)

#### Parameters

- **distributions** (*list*) – List of distributions.
- **prior** (*pixyz.Distribution.Categorical*) – Prior distribution of latent variable (i.e., a contribution rate). This should be a categorical distribution and the number of its category should be the same as the length of *distributions*.
- **name** (*str*, defaults to “p”) – Name of this distribution. This name is displayed in *prob\_text* and *prob\_factorized\_text*.

#### **hidden\_var**

Hidden variables of this distribution.

**Type** *list*

#### **prob\_factorized\_text**

Return a formula of the factorized probability distribution.

**Type** *str*

#### **distribution\_name**

Name of this distribution class.

**Type** *str*

#### **posterior** (*name=None*)

**sample** (*x\_dict={}, batch\_n=None, sample\_shape=torch.Size([]), return\_all=True, return\_hidden=False, \*\*kwargs*)

Sample variables of this distribution. If *cond\_var* is not empty, you should set inputs as dict.

#### Parameters

- **x\_dict** (*torch.Tensor, list, or dict*, defaults to `{}`) – Input variables.
- **batch\_n** (*int*, defaults to `None`.) – Set batch size of parameters.
- **sample\_shape** (*list or NoneType*, defaults to `torch.Size()`) – Shape of generating samples.
- **return\_all** (*bool*, defaults to `True`) – Choose whether the output contains input variables.
- **reparam** (*bool*, defaults to `False`.) – Choose whether we sample variables with re-parameterized trick.

**Returns output** – Samples of this distribution.

**Return type** dict

## Examples

```
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10, 2])
>>> print(p)
Distribution:
  p(x)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([10, 2])
    (loc): torch.Size([1, 10, 2])
    (scale): torch.Size([1, 10, 2])
  )
>>> p.sample()["x"].shape # (batch_n=1, features_shape)
torch.Size([1, 10, 2])
>>> p.sample(batch_n=20)["x"].shape # (batch_n, features_shape)
torch.Size([20, 10, 2])
>>> p.sample(batch_n=20, sample_shape=[40, 30])["x"].shape # (sample_shape,
↪batch_n, features_shape)
torch.Size([40, 30, 20, 10, 2])
```

```
>>> # Conditional distribution
>>> p = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...           features_shape=[10])
>>> print(p)
Distribution:
  p(x|y)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=['y'], input_var=['y'], features_shape=torch.
↪Size([10])
    (scale): torch.Size([1, 10])
  )
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> sample_a = torch.randn(1, 10) # Psuedo data
>>> sample = p.sample({"y": sample_y})
>>> print(sample) # input_var + var # doctest: +SKIP
{'y': tensor([[ -0.5182,  0.3484,  0.9042,  0.1914,  0.6905,
                -1.0859, -0.4433, -0.0255,  0.8198,  0.4571]]),
 'x': tensor([[ -0.7205, -1.3996,  0.5528, -0.3059,  0.5384,
                -1.4976, -0.1480,  0.0841, 0.3321,  0.5561]])}
>>> sample = p.sample({"y": sample_y, "a": sample_a}) # Redundant input ("a")
>>> print(sample) # input_var + var + "a" (redundant input) # doctest: +SKIP
{'y': tensor([[ 1.3582, -1.1151, -0.8111,  1.0630,  1.1633,
                0.3855,  2.6324, -0.9357, -0.8649, -0.6015]]),
 'a': tensor([[ -0.1874,  1.7958, -1.4084, -2.5646,  1.0868,
                -0.7523, -0.0852, -2.4222, -0.3914, -0.9755]]),
 'x': tensor([[ -0.3272, -0.5222, -1.3659,  1.8386,  2.3204,
                0.3686,  0.6311, -1.1208, 0.3656, -0.6683]])}
```



**has\_reparam**

**get\_log\_prob** (*x\_dict*, *return\_hidden=False*, *\*\*kwargs*)

Evaluate log-pdf, log  $p(x)$  (if *return\_hidden=False*) or log  $p(x, z)$  (if *return\_hidden=True*).

**Parameters**

- **x\_dict** (*dict*) – Input variables (including *var*).
- **return\_hidden** (*bool*, defaults to *False*) –

**Returns**

**log\_prob** – The log-pdf value of *x*.

**return\_hidden = 0** : *dim=0* : the size of batch

**return\_hidden = 1** : *dim=0* : the number of mixture

*dim=1* : the size of batch

**Return type** torch.Tensor

## 1.3.2 ProductOfNormal

**class** pixyz.distributions.**ProductOfNormal** (*p=[]*, *name='p'*, *features\_shape=torch.Size([])*, *fea-*  
*Bases:* pixyz.distributions.exponential\_distributions.Normal  
 Product of normal distributions.

$$p(z|x, y) \propto p(z)p(z|x)p(z|y)$$

In this model,  $p(z|x)$  and  $p(a|y)$  perform as *experts* and  $p(z)$  corresponds a prior of *experts*.

### References

[Vedantam+ 2017] Generative Models of Visually Grounded Imagination

[Wu+ 2018] Multimodal Generative Models for Scalable Weakly-Supervised Learning

### Examples

```
>>> pon = ProductOfNormal([p_x, p_y]) # doctest: +SKIP
>>> pon.sample({"x": x, "y": y}) # doctest: +SKIP
{'x': tensor([[0., 0., 0., ..., 0., 0., 0.],
              [0., 0., 0., ..., 0., 0., 0.],
              [0., 0., 0., ..., 0., 0., 0.],
              ...,
              [0., 0., 0., ..., 0., 0., 0.],
              [0., 0., 0., ..., 0., 0., 0.],
              [0., 0., 0., ..., 0., 0., 0.]]),
 'y': tensor([[0., 0., 0., ..., 0., 0., 1.],
              [0., 0., 1., ..., 0., 0., 0.],
              [0., 1., 0., ..., 0., 0., 0.],
              ...,
              [0., 0., 0., ..., 0., 1., 0.],
              [1., 0., 0., ..., 0., 0., 0.]])
```

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```

    [0., 0., 0., ..., 0., 0., 1.])),
    'z': tensor([[ 0.6611,  0.3811,  0.7778, ..., -0.0468, -0.3615, -0.6569],
    [-0.0071, -0.9178,  0.6620, ..., -0.1472,  0.6023,  0.5903],
    [-0.3723, -0.7758,  0.0195, ...,  0.8239, -0.3537,  0.3854],
    ...,
    [ 0.7820, -0.4761,  0.1804, ..., -0.5701, -0.0714, -0.5485],
    [-0.1873, -0.2105, -0.1861, ..., -0.5372,  0.0752,  0.2777],
    [-0.2563, -0.0828,  0.1605, ...,  0.2767, -0.8456,  0.7364]]))
>>> pon.sample({"y": y}) # doctest: +SKIP
{'y': tensor([[0., 0., 0., ..., 0., 0., 0.],
    [0., 0., 0., ..., 0., 0., 1.],
    [0., 0., 0., ..., 1., 0., 0.],
    ...,
    [0., 0., 0., ..., 0., 0., 0.],
    [0., 1., 0., ..., 0., 0., 0.],
    [0., 0., 0., ..., 0., 0., 0.])),
    'z': tensor([[ -0.3264, -0.4448,  0.3610, ..., -0.7378,  0.3002,  0.4370],
    [ 0.0928, -0.1830,  1.1768, ...,  1.1808, -0.7226, -0.4152],
    [ 0.6999,  0.2222, -0.2901, ...,  0.5706,  0.7091,  0.5179],
    ...,
    [ 0.5688, -1.6612, -0.0713, ..., -0.1400, -0.3903,  0.2533],
    [ 0.5412, -0.0289,  0.6365, ...,  0.7407,  0.7838,  0.9218],
    [ 0.0299,  0.5148, -0.1001, ...,  0.9938,  1.0689, -1.1902]])}
>>> pon.sample() # same as sampling from unit Gaussian. # doctest: +SKIP
{'z': tensor(-0.4494)}
```

`__init__` ( $p=[]$ ,  $name='p'$ ,  $features\_shape=torch.Size([])$ )

#### Parameters

- **p** (list of `pixyz.distributions.Normal`) – List of experts.
- **name** (str, defaults to “p”) – Name of this distribution. This name is displayed in `prob_text` and `prob_factorized_text`.
- **features\_shape** (`torch.Size` or list, defaults to `torch.Size()`) – Shape of dimensions (features) of this distribution.

#### Examples

```

>>> p_x = Normal(cond_var=['z'], loc='z', scale=torch.ones(1, 1))
>>> pon = ProductOfNormal([p_x])
>>> sample = pon.sample({'z': torch.zeros(1, 1)})
>>> sample # doctest: +SKIP
```

#### `prob_factorized_text`

Return a formula of the factorized probability distribution.

**Type** str

#### `prob_joint_factorized_and_text`

Return a formula of the factorized probability distribution.

**Type** str

`get_params` ( $params\_dict=\{\}$ ,  $**kwargs$ )

`log_prob` ( $sum\_features=True$ ,  $feature\_dims=None$ )

Return an instance of `pixyz.losses.LogProb`.

**Parameters**

- **sum\_features** (bool, defaults to True) – Whether the output is summed across some axes (dimensions) which are specified by `feature_dims`.
- **feature\_dims** (list or NoneType, defaults to None) – Set axes to sum across the output.

**Returns** An instance of `pixyz.losses.LogProb`

**Return type** `pixyz.losses.LogProb`

**Examples**

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> log_prob = p1.log_prob().eval({"x": sample_x})
>>> print(log_prob) # doctest: +SKIP
tensor([-16.1153])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> log_prob = p2.log_prob().eval({"x": sample_x, "y": sample_y})
>>> print(log_prob) # doctest: +SKIP
tensor([-21.5251])
```

**prob** (`sum_features=True, feature_dims=None`)

Return an instance of `pixyz.losses.Prob`.

**Parameters**

- **sum\_features** (bool, defaults to True) – Choose whether the output is summed across some axes (dimensions) which are specified by `feature_dims`.
- **feature\_dims** (list or NoneType, defaults to None) – Set dimensions to sum across the output. (Note: this parameter is not used for now.)

**Returns** An instance of `pixyz.losses.Prob`

**Return type** `pixyz.losses.Prob`

**Examples**

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> prob = p1.prob().eval({"x": sample_x})
>>> print(prob) # doctest: +SKIP
tensor([4.0933e-07])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> prob = p2.prob().eval({"x": sample_x, "y": sample_y})
>>> print(prob) # doctest: +SKIP
tensor([2.9628e-09])
```

**get\_log\_prob** (*x\_dict*, *sum\_features=True*, *feature\_dims=None*)

Giving variables, this method returns values of log-pdf.

#### Parameters

- **x\_dict** (*dict*) – Input variables.
- **sum\_features** (*bool*, defaults to *True*) – Whether the output is summed across some dimensions which are specified by *feature\_dims*.
- **feature\_dims** (*list* or *NoneType*, defaults to *None*) – Set dimensions to sum across the output.

**Returns** **log\_prob** – Values of log-probability density/mass function.

**Return type** `torch.Tensor`

#### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> log_prob = p1.log_prob({"x": sample_x})
>>> print(log_prob) # doctest: +SKIP
tensor([-16.1153])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> log_prob = p2.log_prob({"x": sample_x, "y": sample_y})
>>> print(log_prob) # doctest: +SKIP
tensor([-21.5251])
```

### 1.3.3 ElementWiseProductOfNormal

**class** `pixyz.distributions.ElementWiseProductOfNormal` (*p*, *name='p'*, *features\_shape=torch.Size([])*)

Bases: `pixyz.distributions.poe.ProductOfNormal`

Product of normal distributions. In this distribution, each element of the input vector on the given distribution is considered as a different expert.

$$p(z|x) = p(z|x_1, x_2) \propto p(z)p(z|x_1)p(z|x_2)$$

## Examples

```
>>> pon = ElementWiseProductOfNormal(p) # doctest: +SKIP
>>> pon.sample({"x": x}) # doctest: +SKIP
{'x': tensor([[0., 0., 1., 0., 0., 0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 1., 0., 0., 0., 0., 0.])),
 'z': tensor([[ -0.3572, -0.0632,  0.4872,  0.2269, -0.1693, -0.0160, -0.0429,  0.
↪2017,
              -0.1589, -0.3380, -0.9598,  0.6216, -0.4296, -1.1349,  0.0901,  0.3994,
              0.2313, -0.5227, -0.7973,  0.3968,  0.7137, -0.5639, -0.4891, -0.1249,
              0.8256,  0.1463,  0.0801, -1.2202,  0.6984, -0.4036,  0.4960, -0.4376,
              0.3310, -0.2243, -0.2381, -0.2200,  0.8969,  0.2674,  0.4681,  1.6764,
              0.8127,  0.2722, -0.2048,  0.1903, -0.1398,  0.0099,  0.4382, -0.8016,
              0.9947,  0.7556, -0.2017, -0.3920,  1.4212, -1.2529, -0.1002, -0.0031,
              0.1876,  0.4267,  0.3622,  0.2648,  0.4752,  0.0843, -0.3065, -0.4922],
              [ 0.3770, -0.0413,  0.9102,  0.2897, -0.0567,  0.5211,  1.5233, -0.3539,
              0.5163, -0.2271, -0.1027,  0.0294, -1.4617,  0.1640,  0.2025, -0.2190,
              0.0555,  0.5779, -0.2930, -0.2161,  0.2835, -0.0354, -0.2569, -0.7171,
              0.0164, -0.4080,  1.1088,  0.3947,  0.2720, -0.0600, -0.9295, -0.0234,
              0.5624,  0.4866,  0.5285,  1.1827,  0.2494,  0.0777,  0.7585,  0.5127,
              0.7500, -0.3253,  0.0250,  0.0888,  1.0340, -0.1405, -0.8114,  0.4492,
              0.2725, -0.0270,  0.6379, -0.8096,  0.4259,  0.3179, -0.1681,  0.3365,
              0.6305,  0.5203,  0.2384,  0.0572,  0.4804,  0.9553, -0.3244,  1.5373]])})
>>> pon.sample({"x": torch.zeros_like(x)}) # same as sampling from unit Gaussian.
↪ # doctest: +SKIP
{'x': tensor([[0., 0., 0., 0., 0., 0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 0., 0., 0., 0., 0., 0.])),
 'z': tensor([[ -0.7777, -0.5908, -1.5498, -0.7505,  0.6201,  0.7218,  1.0045,  0.
↪8923,
              -0.8030, -0.3569,  0.2932,  0.2122,  0.1640,  0.7893, -0.3500, -1.0537,
              -1.2769,  0.6122, -1.0083, -0.2915, -0.1928, -0.7486,  0.2418, -1.9013,
              1.2514,  1.3035, -0.3029, -0.3098, -0.5415,  1.1970, -0.4443,  2.2393,
              -0.6980,  0.2820,  1.6972,  0.6322,  0.4308,  0.8953,  0.7248,  0.4440,
              2.2770,  1.7791,  0.7563, -1.1781, -0.8331,  0.1825,  1.5447,  0.1385,
              -1.1348,  0.0257,  0.3374,  0.5889,  1.1231, -1.2476, -0.3801, -1.4404,
              -1.3066, -1.2653,  0.5958, -1.7423,  0.7189, -0.7236,  0.2330,  0.3117],
              [ 0.5495,  0.7210, -0.4708, -2.0631, -0.6170,  0.2436, -0.0133, -0.4616,
              -0.8091, -0.1592,  1.3117,  0.0276,  0.6625, -0.3748, -0.5049,  1.8260,
              -0.3631,  1.1546, -1.0913,  0.2712,  1.5493,  1.4294, -2.1245, -2.0422,
              0.4976, -1.2785,  0.5028,  1.4240,  1.1983,  0.2468,  1.1682, -0.6725,
              -1.1198, -1.4942, -0.3629,  0.1325, -0.2256,  0.4280,  0.9830, -1.9427,
              -0.2181,  1.1850, -0.7514, -0.8172,  2.1031, -0.1698, -0.3777, -0.7863,
              1.0936, -1.3720,  0.9999,  1.3302, -0.8954, -0.5999,  2.3305,  0.5702,
              -1.0767, -0.2750, -0.3741, -0.7026, -1.5408,  0.0667,  1.2550, -0.5117]])})
```

`__init__(p, name='p', features_shape=torch.Size([]))`

### Parameters

- **p** (`pixyz.distributions.Normal`) – Each element of this input vector is considered as a different expert. When some elements are 0, experts corresponding to these elements are considered not to be specified.  $p(z|x) = p(z|x_1, x_2 = 0) \propto p(z)p(z|x_1)$
- **name** (`str`, defaults to `"p"`) – Name of this distribution. This name is displayed in `prob_text` and `prob_factorized_text`.
- **features\_shape** (`torch.Size` or `list`, defaults to `torch.Size()`) – Shape of dimensions (features) of this distribution.

## 1.4 Flow distributions

### 1.4.1 TransformedDistribution

**class** pixyz.distributions.**TransformedDistribution** (*prior, flow, var, name='p'*)

Bases: *pixyz.distributions.distributions.Distribution*

Convert flow transformations to distributions.

$$p(z = f_{flow}(x)),$$

where  $x \sim p_{prior}(x)$ .

Once initializing, it can be handled as a distribution module.

**distribution\_name**

Name of this distribution class.

**Type** str

**flow\_input\_var**

Input variables of the flow module.

**Type** list

**prob\_factorized\_text**

Return a formula of the factorized probability distribution.

**Type** str

**logdet\_jacobian**

Get log-determinant Jacobian.

Before calling this, you should run *forward* or *update\_jacobian* methods to calculate and store log-determinant Jacobian.

**sample** (*x\_dict={}, batch\_n=None, sample\_shape=torch.Size([]), return\_all=True, reparam=False, compute\_jacobian=True*)

Sample variables of this distribution. If *cond\_var* is not empty, you should set inputs as *dict*.

**Parameters**

- **x\_dict** (*torch.Tensor, list, or dict*, defaults to *{}*) – Input variables.
- **batch\_n** (*int*, defaults to *None*.) – Set batch size of parameters.
- **sample\_shape** (*list or NoneType*, defaults to *torch.Size()*) – Shape of generating samples.
- **return\_all** (*bool*, defaults to *True*) – Choose whether the output contains input variables.
- **reparam** (*bool*, defaults to *False*.) – Choose whether we sample variables with re-parameterized trick.

**Returns output** – Samples of this distribution.

**Return type** dict

## Examples

```
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10, 2])
>>> print(p)
Distribution:
  p(x)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([10, 2])
    (loc): torch.Size([1, 10, 2])
    (scale): torch.Size([1, 10, 2])
  )
>>> p.sample()["x"].shape # (batch_n=1, features_shape)
torch.Size([1, 10, 2])
>>> p.sample(batch_n=20)["x"].shape # (batch_n, features_shape)
torch.Size([20, 10, 2])
>>> p.sample(batch_n=20, sample_shape=[40, 30])["x"].shape # (sample_shape,
↳ batch_n, features_shape)
torch.Size([40, 30, 20, 10, 2])
```

```
>>> # Conditional distribution
>>> p = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...           features_shape=[10])
>>> print(p)
Distribution:
  p(x|y)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=['y'], input_var=['y'], features_shape=torch.
↳ Size([10])
    (scale): torch.Size([1, 10])
  )
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> sample_a = torch.randn(1, 10) # Psuedo data
>>> sample = p.sample({"y": sample_y})
>>> print(sample) # input_var + var # doctest: +SKIP
{'y': tensor([[ -0.5182,  0.3484,  0.9042,  0.1914,  0.6905,
                -1.0859, -0.4433, -0.0255,  0.8198,  0.4571]]),
 'x': tensor([[ -0.7205, -1.3996,  0.5528, -0.3059,  0.5384,
                -1.4976, -0.1480,  0.0841, 0.3321,  0.5561]])}
>>> sample = p.sample({"y": sample_y, "a": sample_a}) # Redundant input ("a")
>>> print(sample) # input_var + var + "a" (redundant input) # doctest: +SKIP
{'y': tensor([[ 1.3582, -1.1151, -0.8111,  1.0630,  1.1633,
                0.3855,  2.6324, -0.9357, -0.8649, -0.6015]]),
 'a': tensor([[ -0.1874,  1.7958, -1.4084, -2.5646,  1.0868,
                -0.7523, -0.0852, -2.4222, -0.3914, -0.9755]]),
 'x': tensor([[ -0.3272, -0.5222, -1.3659,  1.8386,  2.3204,
                0.3686,  0.6311, -1.1208, 0.3656, -0.6683]])}
```

### has\_reparam

**get\_log\_prob** (*x\_dict*, *sum\_features=True*, *feature\_dims=None*, *compute\_jacobian=False*)

It calculates the log-likelihood for a given *z*. If a flow module has no inverse method, it only supports the

previously sampled  $z$ -values.

**forward** ( $x$ ,  $y=None$ ,  $compute\_jacobian=True$ )

Forward propagation of flow layers.

**Parameters**

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.
- **compute\_jacobian** (*bool*, defaults to *True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in *logdet\_jacobian*.

**Returns z**

**Return type** torch.Tensor

**inverse** ( $z$ ,  $y=None$ )

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

**Parameters**

- **z** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.

**Returns x**

**Return type** torch.Tensor

## 1.4.2 InverseTransformedDistribution

```
class pixyz.distributions.InverseTransformedDistribution (prior, flow, var,  
                                                         cond_var=[],  
                                                         name='p')
```

Bases: *pixyz.distributions.distributions.Distribution*

Convert inverse flow transformations to distributions.

$$p(x = f_{flow}^{-1}(z)),$$

where  $z \sim p_{prior}(z)$ .

Once initializing, it can be handled as a distribution module.

Moreover, this distribution can take a conditional variable.

$$p(x = f_{flow}^{-1}(z, y)),$$

where  $z \sim p_{prior}(z)$  and  $y$  is given.

**distribution\_name**

Name of this distribution class.

**Type** str

**flow\_output\_var**

**prob\_factorized\_text**

Return a formula of the factorized probability distribution.

**Type** str



**logdet\_jacobian**

Get log-determinant Jacobian.

Before calling this, you should run `forward` or `update_jacobian` methods to calculate and store log-determinant Jacobian.

**sample** (*x\_dict*={}, *batch\_n*=None, *sample\_shape*=torch.Size([]), *return\_all*=True, *reparam*=False, *return\_hidden*=True)

Sample variables of this distribution. If *cond\_var* is not empty, you should set inputs as dict.

**Parameters**

- **x\_dict** (torch.Tensor, list, or dict, defaults to {}) – Input variables.
- **batch\_n** (int, defaults to None.) – Set batch size of parameters.
- **sample\_shape** (list or NoneType, defaults to torch.Size()) – Shape of generating samples.
- **return\_all** (bool, defaults to True) – Choose whether the output contains input variables.
- **reparam** (bool, defaults to False.) – Choose whether we sample variables with re-parameterized trick.

**Returns** **output** – Samples of this distribution.

**Return type** dict

**Examples**

```
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10, 2])
>>> print(p)
Distribution:
  p(x)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([10, 2])
    (loc): torch.Size([1, 10, 2])
    (scale): torch.Size([1, 10, 2])
  )
>>> p.sample()["x"].shape # (batch_n=1, features_shape)
torch.Size([1, 10, 2])
>>> p.sample(batch_n=20)["x"].shape # (batch_n, features_shape)
torch.Size([20, 10, 2])
>>> p.sample(batch_n=20, sample_shape=[40, 30])["x"].shape # (sample_shape,
↪batch_n, features_shape)
torch.Size([40, 30, 20, 10, 2])
```

```
>>> # Conditional distribution
>>> p = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...           features_shape=[10])
>>> print(p)
Distribution:
  p(x|y)
```

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```

Network architecture:
    Normal(
        name=p, distribution_name=Normal,
        var=['x'], cond_var=['y'], input_var=['y'], features_shape=torch.
↪Size([10])
        (scale): torch.Size([1, 10])
    )
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> sample_a = torch.randn(1, 10) # Psuedo data
>>> sample = p.sample({"y": sample_y})
>>> print(sample) # input_var + var # doctest: +SKIP
{'y': tensor([[ -0.5182,  0.3484,  0.9042,  0.1914,  0.6905,
                -1.0859, -0.4433, -0.0255,  0.8198,  0.4571]]),
 'x': tensor([[ -0.7205, -1.3996,  0.5528, -0.3059,  0.5384,
                -1.4976, -0.1480,  0.0841, 0.3321,  0.5561]])}
>>> sample = p.sample({"y": sample_y, "a": sample_a}) # Redundant input ("a")
>>> print(sample) # input_var + var + "a" (redundant input) # doctest: +SKIP
{'y': tensor([[ 1.3582, -1.1151, -0.8111,  1.0630,  1.1633,
                0.3855,  2.6324, -0.9357, -0.8649, -0.6015]]),
 'a': tensor([[ -0.1874,  1.7958, -1.4084, -2.5646,  1.0868,
                -0.7523, -0.0852, -2.4222, -0.3914, -0.9755]]),
 'x': tensor([[ -0.3272, -0.5222, -1.3659,  1.8386,  2.3204,
                0.3686,  0.6311, -1.1208,  0.3656, -0.6683]])}

```

**has\_reparam****inference** (*x\_dict*, *return\_all=True*, *compute\_jacobian=False*)**get\_log\_prob** (*x\_dict*, *sum\_features=True*, *feature\_dims=None*)

Giving variables, this method returns values of log-pdf.

**Parameters**

- **x\_dict** (*dict*) – Input variables.
- **sum\_features** (*bool*, defaults to *True*) – Whether the output is summed across some dimensions which are specified by *feature\_dims*.
- **feature\_dims** (*list* or *NoneType*, defaults to *None*) – Set dimensions to sum across the output.

**Returns log\_prob** – Values of log-probability density/mass function.**Return type** `torch.Tensor`**Examples**

```

>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> log_prob = p1.log_prob({"x": sample_x})
>>> print(log_prob) # doctest: +SKIP
tensor([-16.1153])

```

```

>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> log_prob = p2.log_prob({"x": sample_x, "y": sample_y})
>>> print(log_prob) # doctest: +SKIP
tensor([-21.5251])

```

**forward** (*x*, *y=None*, *compute\_jacobian=True*)

Forward propagation of flow layers.

#### Parameters

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.
- **compute\_jacobian** (*bool*, defaults to *True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in *logdet\_jacobian*.

**Returns** *z*

**Return type** *torch.Tensor*

**inverse** (*z*, *y=None*)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

#### Parameters

- **z** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.

**Returns** *x*

**Return type** *torch.Tensor*

## 1.5 Special distributions

### 1.5.1 Deterministic

**class** *pixyz.distributions.Deterministic* (*var*, *cond\_var=[]*, *name='p'*, *\*\*kwargs*)

Bases: *pixyz.distributions.distributions.Distribution*

Deterministic distribution (or degeneration distribution)

#### Examples

```

>>> import torch
>>> class Generator(Deterministic):
...     def __init__(self):
...         super().__init__(var=["x"], cond_var=["z"])
...         self.model = torch.nn.Linear(64, 512)
...     def forward(self, z):
...         return {"x": self.model(z)}
>>> p = Generator()

```

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```

>>> print(p)
Distribution:
  p(x|z)
Network architecture:
  Generator(
    name=p, distribution_name=Deterministic,
    var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
    (model): Linear(in_features=64, out_features=512, bias=True)
  )
>>> sample = p.sample({"z": torch.randn(1, 64)})
>>> p.log_prob().eval(sample) # log_prob is not defined.
Traceback (most recent call last):
...
NotImplementedError: Log probability of deterministic distribution is not defined.

```

**distribution\_name**

Name of this distribution class.

**Type** str**sample** (x\_dict={}, return\_all=True, \*\*kwargs)

Sample variables of this distribution. If cond\_var is not empty, you should set inputs as dict.

**Parameters**

- **x\_dict** (torch.Tensor, list, or dict, defaults to {}) – Input variables.
- **batch\_n** (int, defaults to None.) – Set batch size of parameters.
- **sample\_shape** (list or NoneType, defaults to torch.Size()) – Shape of generating samples.
- **return\_all** (bool, defaults to True) – Choose whether the output contains input variables.
- **reparam** (bool, defaults to False.) – Choose whether we sample variables with re-parameterized trick.

**Returns output** – Samples of this distribution.**Return type** dict**Examples**

```

>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10, 2])
>>> print(p)
Distribution:
  p(x)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([10, 2])
    (loc): torch.Size([1, 10, 2])
    (scale): torch.Size([1, 10, 2])
  )

```

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```
>>> p.sample()["x"].shape # (batch_n=1, features_shape)
torch.Size([1, 10, 2])
>>> p.sample(batch_n=20)["x"].shape # (batch_n, features_shape)
torch.Size([20, 10, 2])
>>> p.sample(batch_n=20, sample_shape=[40, 30])["x"].shape # (sample_shape,
↪batch_n, features_shape)
torch.Size([40, 30, 20, 10, 2])
```

```
>>> # Conditional distribution
>>> p = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...           features_shape=[10])
>>> print(p)
Distribution:
  p(x|y)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=['y'], input_var='y', features_shape=torch.
↪Size([10])
    (scale): torch.Size([1, 10])
  )
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> sample_a = torch.randn(1, 10) # Psuedo data
>>> sample = p.sample({"y": sample_y})
>>> print(sample) # input_var + var # doctest: +SKIP
{'y': tensor([[ -0.5182,  0.3484,  0.9042,  0.1914,  0.6905,
                -1.0859, -0.4433, -0.0255,  0.8198,  0.4571]]),
 'x': tensor([[ -0.7205, -1.3996,  0.5528, -0.3059,  0.5384,
                -1.4976, -0.1480,  0.0841, 0.3321,  0.5561]])}
>>> sample = p.sample({"y": sample_y, "a": sample_a}) # Redundant input ("a")
>>> print(sample) # input_var + var + "a" (redundant input) # doctest: +SKIP
{'y': tensor([[ 1.3582, -1.1151, -0.8111,  1.0630,  1.1633,
                0.3855,  2.6324, -0.9357, -0.8649, -0.6015]]),
 'a': tensor([[ -0.1874,  1.7958, -1.4084, -2.5646,  1.0868,
                -0.7523, -0.0852, -2.4222, -0.3914, -0.9755]]),
 'x': tensor([[ -0.3272, -0.5222, -1.3659,  1.8386,  2.3204,
                0.3686,  0.6311, -1.1208, 0.3656, -0.6683]])}
```

**sample\_mean** (*x\_dict*)

Return the mean of the distribution.

**Parameters** *x\_dict* (dict, defaults to {}) – Parameters of this distribution.**Examples**

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10], name="p1")
>>> mean = p1.sample_mean()
>>> print(mean)
tensor([[0., 0., 0., 0., 0., 0., 0., 0., 0.]])
```

```

>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> mean = p2.sample_mean({"y": sample_y})
>>> print(mean) # doctest: +SKIP
tensor([[ -0.2189, -1.0310, -0.1917, -0.3085,  1.5190, -0.9037,  1.2559,  0.
↪1410,
          1.2810, -0.6681]])

```

**get\_log\_prob** (*x\_dict*, *sum\_features=True*, *feature\_dims=None*)

Giving variables, this method returns values of log-pdf.

#### Parameters

- **x\_dict** (*dict*) – Input variables.
- **sum\_features** (*bool*, defaults to *True*) – Whether the output is summed across some dimensions which are specified by *feature\_dims*.
- **feature\_dims** (*list* or *NoneType*, defaults to *None*) – Set dimensions to sum across the output.

**Returns** **log\_prob** – Values of log-probability density/mass function.

**Return type** `torch.Tensor`

#### Examples

```

>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> log_prob = p1.log_prob({"x": sample_x})
>>> print(log_prob) # doctest: +SKIP
tensor([-16.1153])

```

```

>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> log_prob = p2.log_prob({"x": sample_x, "y": sample_y})
>>> print(log_prob) # doctest: +SKIP
tensor([-21.5251])

```

**has\_reparam**

## 1.5.2 EmpiricalDistribution

**class** `pixyz.distributions.EmpiricalDistribution` (*var*, *name='p\_{data}'*)

Bases: `pixyz.distributions.distributions.Distribution`

Data distribution.

Samples from this distribution equal given inputs.

## Examples

```
>>> import torch
>>> p = EmpiricalDistribution(var=["x"])
>>> print(p)
Distribution:
  p_{data}(x)
Network architecture:
  EmpiricalDistribution(
    name=p_{data}, distribution_name=Data distribution,
    var=['x'], cond_var=[], input_var=['x'], features_shape=torch.Size([])
  )
>>> sample = p.sample({"x": torch.randn(1, 64)})
```

### **distribution\_name**

Name of this distribution class.

**Type** str

**sample** (*x\_dict*={}, *return\_all*=True, *\*\*kwargs*)

Sample variables of this distribution. If *cond\_var* is not empty, you should set inputs as dict.

### **Parameters**

- **x\_dict** (torch.Tensor, list, or dict, defaults to {}) – Input variables.
- **batch\_n** (int, defaults to None.) – Set batch size of parameters.
- **sample\_shape** (list or NoneType, defaults to torch.Size()) – Shape of generating samples.
- **return\_all** (bool, defaults to True) – Choose whether the output contains input variables.
- **reparam** (bool, defaults to False.) – Choose whether we sample variables with reparameterized trick.

**Returns** output – Samples of this distribution.

**Return type** dict

## Examples

```
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10, 2])
>>> print(p)
Distribution:
  p(x)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([10, 2])
    (loc): torch.Size([1, 10, 2])
    (scale): torch.Size([1, 10, 2])
  )
>>> p.sample()["x"].shape # (batch_n=1, features_shape)
torch.Size([1, 10, 2])
```

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```
>>> p.sample(batch_n=20)["x"].shape # (batch_n, features_shape)
torch.Size([20, 10, 2])
>>> p.sample(batch_n=20, sample_shape=[40, 30])["x"].shape # (sample_shape,
↪batch_n, features_shape)
torch.Size([40, 30, 20, 10, 2])
```

```
>>> # Conditional distribution
>>> p = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...           features_shape=[10])
>>> print(p)
Distribution:
  p(x|y)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=['y'], input_var=['y'], features_shape=torch.
↪Size([10])
    (scale): torch.Size([1, 10])
  )
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> sample_a = torch.randn(1, 10) # Psuedo data
>>> sample = p.sample({"y": sample_y})
>>> print(sample) # input_var + var # doctest: +SKIP
{'y': tensor([[ -0.5182,  0.3484,  0.9042,  0.1914,  0.6905,
                -1.0859, -0.4433, -0.0255,  0.8198,  0.4571]]),
 'x': tensor([[ -0.7205, -1.3996,  0.5528, -0.3059,  0.5384,
                -1.4976, -0.1480,  0.0841, 0.3321,  0.5561]])}
>>> sample = p.sample({"y": sample_y, "a": sample_a}) # Redundant input ("a")
>>> print(sample) # input_var + var + "a" (redundant input) # doctest: +SKIP
{'y': tensor([[ 1.3582, -1.1151, -0.8111,  1.0630,  1.1633,
                0.3855,  2.6324, -0.9357, -0.8649, -0.6015]]),
 'a': tensor([[ -0.1874,  1.7958, -1.4084, -2.5646,  1.0868,
                -0.7523, -0.0852, -2.4222, -0.3914, -0.9755]]),
 'x': tensor([[ -0.3272, -0.5222, -1.3659,  1.8386,  2.3204,
                0.3686,  0.6311, -1.1208, 0.3656, -0.6683]])}
```

**sample\_mean** (*x\_dict*)

Return the mean of the distribution.

**Parameters** *x\_dict* (dict, defaults to {}) – Parameters of this distribution.**Examples**

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10], name="p1")
>>> mean = p1.sample_mean()
>>> print(mean)
tensor([[0., 0., 0., 0., 0., 0., 0., 0., 0.]])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...           features_shape=[10], name="p2")
```

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```
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> mean = p2.sample_mean({"y": sample_y})
>>> print(mean) # doctest: +SKIP
tensor([[ -0.2189, -1.0310, -0.1917, -0.3085,  1.5190, -0.9037,  1.2559,  0.
↪1410,
          1.2810, -0.6681]])
```

**get\_log\_prob** (*x\_dict*, *sum\_features=True*, *feature\_dims=None*)

Giving variables, this method returns values of log-pdf.

#### Parameters

- **x\_dict** (*dict*) – Input variables.
- **sum\_features** (*bool*, defaults to *True*) – Whether the output is summed across some dimensions which are specified by *feature\_dims*.
- **feature\_dims** (*list* or *NoneType*, defaults to *None*) – Set dimensions to sum across the output.

**Returns** **log\_prob** – Values of log-probability density/mass function.

**Return type** `torch.Tensor`

#### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> log_prob = p1.log_prob({"x": sample_x})
>>> print(log_prob) # doctest: +SKIP
tensor([-16.1153])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> log_prob = p2.log_prob({"x": sample_x, "y": sample_y})
>>> print(log_prob) # doctest: +SKIP
tensor([-21.5251])
```

#### input\_var

In `EmpiricalDistribution`, *input\_var* is same as *var*.

#### has\_reparam

### 1.5.3 CustomProb

**class** `pixyz.distributions.CustomProb` (*log\_prob\_function*, *var*, *distribution\_name='Custom PDF'*, *\*\*kwargs*)

Bases: `pixyz.distributions.distributions.Distribution`

This distribution is constructed by user-defined probability density/mass function.

Note that this distribution cannot perform sampling.

## Examples

```
>>> import torch
>>> # banana shaped distribution
>>> def log_prob(z):
...     z1, z2 = torch.chunk(z, chunks=2, dim=1)
...     norm = torch.sqrt(z1 ** 2 + z2 ** 2)
...     exp1 = torch.exp(-0.5 * ((z1 - 2) / 0.6) ** 2)
...     exp2 = torch.exp(-0.5 * ((z1 + 2) / 0.6) ** 2)
...     u = 0.5 * ((norm - 2) / 0.4) ** 2 - torch.log(exp1 + exp2)
...     return -u
...
>>> p = CustomProb(log_prob, var=["z"])
>>> loss = p.log_prob().eval({"z": torch.randn(10, 2)})
```

`__init__(log_prob_function, var, distribution_name='Custom PDF', **kwargs)`

### Parameters

- **log\_prob\_function** (*function*) – User-defined log-probability density/mass function.
- **var** (*list*) – Variables of this distribution.
- **distribution\_name** (*str*, optional) – Name of this distribution.
- **\*\*kwargs** – Arbitrary keyword arguments.

### log\_prob\_function

User-defined log-probability density/mass function.

### input\_var

Input variables of this distribution. Normally, it has same values as `cond_var`.

**Type** list

### distribution\_name

Name of this distribution class.

**Type** str

### get\_log\_prob(x\_dict, sum\_features=True, feature\_dims=None)

Giving variables, this method returns values of log-pdf.

### Parameters

- **x\_dict** (*dict*) – Input variables.
- **sum\_features** (*bool*, defaults to True) – Whether the output is summed across some dimensions which are specified by *feature\_dims*.
- **feature\_dims** (*list* or *NoneType*, defaults to None) – Set dimensions to sum across the output.

**Returns** **log\_prob** – Values of log-probability density/mass function.

**Return type** torch.Tensor

## Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> sample_x = torch.randn(1, 10) # Psuedo data
>>> log_prob = p1.log_prob({"x": sample_x})
>>> print(log_prob) # doctest: +SKIP
tensor([-16.1153])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> log_prob = p2.log_prob({"x": sample_x, "y": sample_y})
>>> print(log_prob) # doctest: +SKIP
tensor([-21.5251])
```

**sample** (*x\_dict*={}, *return\_all*=True, *\*\*kwargs*)

Sample variables of this distribution. If *cond\_var* is not empty, you should set inputs as dict.

### Parameters

- **x\_dict** (torch.Tensor, list, or dict, defaults to {}) – Input variables.
- **batch\_n** (int, defaults to None.) – Set batch size of parameters.
- **sample\_shape** (list or NoneType, defaults to torch.Size()) – Shape of generating samples.
- **return\_all** (bool, defaults to True) – Choose whether the output contains input variables.
- **reparam** (bool, defaults to False.) – Choose whether we sample variables with re-parameterized trick.

**Returns** **output** – Samples of this distribution.

**Return type** dict

## Examples

```
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...            features_shape=[10, 2])
>>> print(p)
Distribution:
  p(x)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=[], input_var=[], features_shape=torch.Size([10, 2])
    (loc): torch.Size([1, 10, 2])
    (scale): torch.Size([1, 10, 2])
  )
```

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```
>>> p.sample()["x"].shape # (batch_n=1, features_shape)
torch.Size([1, 10, 2])
>>> p.sample(batch_n=20)["x"].shape # (batch_n, features_shape)
torch.Size([20, 10, 2])
>>> p.sample(batch_n=20, sample_shape=[40, 30])["x"].shape # (sample_shape,
↪batch_n, features_shape)
torch.Size([40, 30, 20, 10, 2])
```

```
>>> # Conditional distribution
>>> p = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...           features_shape=[10])
>>> print(p)
Distribution:
  p(x|y)
Network architecture:
  Normal(
    name=p, distribution_name=Normal,
    var=['x'], cond_var=['y'], input_var=['y'], features_shape=torch.
↪Size([10])
    (scale): torch.Size([1, 10])
  )
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> sample_a = torch.randn(1, 10) # Psuedo data
>>> sample = p.sample({"y": sample_y})
>>> print(sample) # input_var + var # doctest: +SKIP
{'y': tensor([[ -0.5182,  0.3484,  0.9042,  0.1914,  0.6905,
                -1.0859, -0.4433, -0.0255,  0.8198,  0.4571]]),
 'x': tensor([[ -0.7205, -1.3996,  0.5528, -0.3059,  0.5384,
                -1.4976, -0.1480,  0.0841, 0.3321,  0.5561]])}
>>> sample = p.sample({"y": sample_y, "a": sample_a}) # Redundant input ("a")
>>> print(sample) # input_var + var + "a" (redundant input) # doctest: +SKIP
{'y': tensor([[ 1.3582, -1.1151, -0.8111,  1.0630,  1.1633,
                0.3855,  2.6324, -0.9357, -0.8649, -0.6015]]),
 'a': tensor([[ -0.1874,  1.7958, -1.4084, -2.5646,  1.0868,
                -0.7523, -0.0852, -2.4222, -0.3914, -0.9755]]),
 'x': tensor([[ -0.3272, -0.5222, -1.3659,  1.8386,  2.3204,
                0.3686,  0.6311, -1.1208,  0.3656, -0.6683]])}
```

**has\_reparam**

## 1.6 Operators

### 1.6.1 ReplaceVarDistribution

**class** pixyz.distributions.**ReplaceVarDistribution**(p, replace\_dict)

Bases: `pixyz.distributions.distributions.Distribution`

Replace names of variables in Distribution.

#### Examples

```

>>> p = DistributionBase(var=["x"], cond_var=["z"])
>>> print(p)
Distribution:
  p(x|z)
Network architecture:
  DistributionBase(
    name=p, distribution_name=,
    var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
  )
>>> replace_dict = {'x': 'y'}
>>> p_repl = ReplaceVarDistribution(p, replace_dict)
>>> print(p_repl)
Distribution:
  p(y|z)
Network architecture:
  p(y|z) -> p(x|z):
  DistributionBase(
    name=p, distribution_name=,
    var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
  )

```

**\_\_init\_\_** (p, replace\_dict)

#### Parameters

- **p** (pixyz.distributions.Distribution (not *pixyz.distributions.MultiplyDistribution*)) – Distribution.
- **replace\_dict** (dict) – Dictionary.

**forward** (\*args, \*\*kwargs)

When this class is inherited by DNNs, this method should be overridden.

**sample\_mean** (x\_dict={})

Return the mean of the distribution.

**Parameters x\_dict** (dict, defaults to {}) – Parameters of this distribution.

#### Examples

```

>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> mean = p1.sample_mean()
>>> print(mean)
tensor([[0., 0., 0., 0., 0., 0., 0., 0., 0., 0.]])

```

```

>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> mean = p2.sample_mean({"y": sample_y})
>>> print(mean) # doctest: +SKIP
tensor([[ -0.2189, -1.0310, -0.1917, -0.3085,  1.5190, -0.9037,  1.2559,  0.
↪1410,
          1.2810, -0.6681]])

```

**sample\_variance** (*x\_dict*={})

Return the variance of the distribution.

**Parameters** **x\_dict** (dict, defaults to {}) – Parameters of this distribution.

### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> var = p1.sample_variance()
>>> print(var)
tensor([[1., 1., 1., 1., 1., 1., 1., 1., 1., 1.]])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> var = p2.sample_variance({"y": sample_y})
>>> print(var) # doctest: +SKIP
tensor([[1., 1., 1., 1., 1., 1., 1., 1., 1., 1.]])
```

**get\_entropy** (*x\_dict*={}, *sum\_features*=True, *feature\_dims*=None)

Giving variables, this method returns values of entropy.

#### Parameters

- **x\_dict** (dict, defaults to {}) – Input variables.
- **sum\_features** (bool, defaults to True) – Whether the output is summed across some dimensions which are specified by *feature\_dims*.
- **feature\_dims** (list or NoneType, defaults to None) – Set dimensions to sum across the output.

**Returns** **entropy** – Values of entropy.

**Return type** torch.Tensor

### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> entropy = p1.get_entropy()
>>> print(entropy)
tensor([14.1894])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
```

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```
>>> entropy = p2.get_entropy({"y": sample_y})
>>> print(entropy)
tensor([14.1894])
```

**distribution\_name**

Name of this distribution class.

**Type** str

## 1.6.2 MarginalizeVarDistribution

**class** pixyz.distributions.**MarginalizeVarDistribution**(p:  
*pixyz.distributions.distributions.Distribution,*  
*marginalize\_list*)

Bases: *pixyz.distributions.distributions.Distribution*

Marginalize variables in Distribution.

$$p(x) = \int p(x, z) dz$$

### Examples

```
>>> a = DistributionBase(var=["x"], cond_var=["z"])
>>> b = DistributionBase(var=["y"], cond_var=["z"])
>>> p_multi = a * b
>>> print(p_multi)
Distribution:
  p(x,y|z) = p(x|z)p(y|z)
Network architecture:
  p(y|z):
  DistributionBase(
    name=p, distribution_name=,
    var=['y'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
  )
  p(x|z):
  DistributionBase(
    name=p, distribution_name=,
    var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
  )
>>> p_marg = MarginalizeVarDistribution(p_multi, ["y"])
>>> print(p_marg)
Distribution:
  p(x|z) = \int p(x|z)p(y|z)dy
Network architecture:
  p(y|z):
  DistributionBase(
    name=p, distribution_name=,
    var=['y'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
  )
  p(x|z):
  DistributionBase(
    name=p, distribution_name=,
    var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
  )
```

`__init__` (*p*: `pixyz.distributions.distributions.Distribution`, *marginalize\_list*)

#### Parameters

- **p** (`pixyz.distributions.Distribution` (not `pixyz.distributions.DistributionBase`)) – `Distribution`.
- **marginalize\_list** (*list*) – Variables to marginalize.

**forward** (*\*args*, *\*\*kwargs*)

When this class is inherited by DNNs, this method should be overridden.

**sample\_mean** (*x\_dict*={})

Return the mean of the distribution.

**Parameters** **x\_dict** (dict, defaults to {}) – Parameters of this distribution.

#### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> mean = p1.sample_mean()
>>> print(mean)
tensor([[0., 0., 0., 0., 0., 0., 0., 0., 0., 0.]])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> mean = p2.sample_mean({"y": sample_y})
>>> print(mean) # doctest: +SKIP
tensor([[ -0.2189, -1.0310, -0.1917, -0.3085,  1.5190, -0.9037,  1.2559,  0.
↪1410,
         1.2810, -0.6681]])
```

**sample\_variance** (*x\_dict*={})

Return the variance of the distribution.

**Parameters** **x\_dict** (dict, defaults to {}) – Parameters of this distribution.

#### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> var = p1.sample_variance()
>>> print(var)
tensor([[1., 1., 1., 1., 1., 1., 1., 1., 1., 1.]])
```

```
>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
```

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```

...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> var = p2.sample_variance({"y": sample_y})
>>> print(var) # doctest: +SKIP
tensor([[1., 1., 1., 1., 1., 1., 1., 1., 1., 1.]])

```

**get\_entropy** (*x\_dict*={}, *sum\_features*=True, *feature\_dims*=None)

Giving variables, this method returns values of entropy.

#### Parameters

- **x\_dict** (*dict*, defaults to {}) – Input variables.
- **sum\_features** (*bool*, defaults to True) – Whether the output is summed across some dimensions which are specified by *feature\_dims*.
- **feature\_dims** (*list* or *NoneType*, defaults to None) – Set dimensions to sum across the output.

**Returns** **entropy** – Values of entropy.

**Return type** torch.Tensor

#### Examples

```

>>> import torch
>>> from pixyz.distributions import Normal
>>> # Marginal distribution
>>> p1 = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...             features_shape=[10], name="p1")
>>> entropy = p1.get_entropy()
>>> print(entropy)
tensor([14.1894])

```

```

>>> # Conditional distribution
>>> p2 = Normal(loc="y", scale=torch.tensor(1.), var=["x"], cond_var=["y"],
...             features_shape=[10], name="p2")
>>> sample_y = torch.randn(1, 10) # Psuedo data
>>> entropy = p2.get_entropy({"y": sample_y})
>>> print(entropy)
tensor([14.1894])

```

**distribution\_name**

Name of this distribution class.

**Type** str

### 1.6.3 MultiplyDistribution

**class** pixyz.distributions.**MultiplyDistribution** (*a*, *b*)

Bases: *pixyz.distributions.distributions.Distribution*

Multiply by given distributions, e.g.  $p(x, y|z) = p(x|z, y)p(y|z)$ . In this class, it is checked if two distributions can be multiplied.

$p(x|z)p(z|y)$  -> Valid

$p(x|z)p(y|z)$  -> Valid  
 $p(x|z)p(y|a)$  -> Valid  
 $p(x|z)p(z|x)$  -> Invalid (recursive)  
 $p(x|z)p(x|y)$  -> Invalid (conflict)

## Examples

```
>>> a = DistributionBase(var=["x"],cond_var=["z"])
>>> b = DistributionBase(var=["z"],cond_var=["y"])
>>> p_multi = MultiplyDistribution(a, b)
>>> print(p_multi)
Distribution:
  p(x,z|y) = p(x|z)p(z|y)
Network architecture:
  p(z|y):
    DistributionBase(
      name=p, distribution_name=,
      var=['z'], cond_var=['y'], input_var=['y'], features_shape=torch.Size([])
    )
  p(x|z):
    DistributionBase(
      name=p, distribution_name=,
      var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
    )
>>> b = DistributionBase(var=["y"],cond_var=["z"])
>>> p_multi = MultiplyDistribution(a, b)
>>> print(p_multi)
Distribution:
  p(x,y|z) = p(x|z)p(y|z)
Network architecture:
  p(y|z):
    DistributionBase(
      name=p, distribution_name=,
      var=['y'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
    )
  p(x|z):
    DistributionBase(
      name=p, distribution_name=,
      var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
    )
>>> b = DistributionBase(var=["y"],cond_var=["a"])
>>> p_multi = MultiplyDistribution(a, b)
>>> print(p_multi)
Distribution:
  p(x,y|z,a) = p(x|z)p(y|a)
Network architecture:
  p(y|a):
    DistributionBase(
      name=p, distribution_name=,
      var=['y'], cond_var=['a'], input_var=['a'], features_shape=torch.Size([])
    )
  p(x|z):
    DistributionBase(
      name=p, distribution_name=,
```

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```
var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
)
```

```
__init__(a, b)
```

**Parameters**

- **a** (*pixyz.Distribution*) – Distribution.
- **b** (*pixyz.Distribution*) – Distribution.



## 2.1 Loss

**class** pixyz.losses.losses.**Loss** (*input\_var=None*)

Bases: torch.nn.modules.module.Module

Loss class. In Pixyz, all loss classes are required to inherit this class.

### Examples

```
>>> import torch
>>> from torch.nn import functional as F
>>> from pixyz.distributions import Bernoulli, Normal
>>> from pixyz.losses import KullbackLeibler
...
>>> # Set distributions
>>> class Inference(Normal):
...     def __init__(self):
...         super().__init__(var=["z"], cond_var=["x"], name="q")
...         self.model_loc = torch.nn.Linear(128, 64)
...         self.model_scale = torch.nn.Linear(128, 64)
...     def forward(self, x):
...         return {"loc": self.model_loc(x), "scale": F.softplus(self.model_
↪scale(x))}
...
>>> class Generator(Bernoulli):
...     def __init__(self):
...         super().__init__(var=["x"], cond_var=["z"], name="p")
...         self.model = torch.nn.Linear(64, 128)
...     def forward(self, z):
...         return {"probs": torch.sigmoid(self.model(z))}
...
>>> p = Generator()
```

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```

>>> q = Inference()
>>> prior = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.),
...                 var=["z"], features_shape=[64], name="p_{prior}")
...
>>> # Define a loss function (VAE)
>>> reconst = -p.log_prob().expectation(q)
>>> kl = KullbackLeibler(q,prior)
>>> loss_cls = (reconst - kl).mean()
>>> print(loss_cls)
mean \left(- D_{\text{KL}} \left[q(z|x) || p_{\text{prior}}(z) \right] - \mathbb{E}_{q(z|x)} \left[ \log p(x|z) \right] \right)
>>> # Evaluate this loss function
>>> data = torch.randn(1, 128) # Pseudo data
>>> loss = loss_cls.eval({"x": data})
>>> print(loss) # doctest: +SKIP
tensor(65.5939, grad_fn=<MeanBackward0>)

```

**\_\_init\_\_** (*input\_var=None*)

**Parameters** **input\_var** (list of str, defaults to None) – Input variables of this loss function. In general, users do not need to set them explicitly because these depend on the given distributions and each loss function.

**input\_var**

Input variables of this distribution.

**Type** list

**loss\_text**

**abs()**

Return an instance of `pixyz.losses.losses.AbsLoss`.

**Returns** An instance of `pixyz.losses.losses.AbsLoss`

**Return type** `pixyz.losses.losses.AbsLoss`

**mean()**

Return an instance of `pixyz.losses.losses.BatchMean`.

**Returns** An instance of `pixyz.losses.BatchMean`

**Return type** `pixyz.losses.losses.BatchMean`

**sum()**

Return an instance of `pixyz.losses.losses.BatchSum`.

**Returns** An instance of `pixyz.losses.losses.BatchSum`

**Return type** `pixyz.losses.losses.BatchSum`

**detach()**

Return an instance of `pixyz.losses.losses.Detach`.

**Returns** An instance of `pixyz.losses.losses.Detach`

**Return type** `pixyz.losses.losses.Detach`

**expectation** (*p, sample\_shape=torch.Size([1])*)

Return an instance of `pixyz.losses.Expectation`.

**Parameters**

- **p** (*pixyz.distributions.Distribution*) – Distribution for sampling.
- **sample\_shape** (list or *NoneType*, defaults to *torch.Size()*) – Shape of generating samples.

**Returns** An instance of *pixyz.losses.Expectation*

**Return type** *pixyz.losses.Expectation*

**constant\_var** (*constant\_dict*)

Return an instance of *pixyz.losses.ConstantVar*.

**Parameters** **constant\_dict** (*dict*) – constant variables.

**Returns** An instance of *pixyz.losses.ConstantVar*

**Return type** *pixyz.losses.ConstantVar*

**eval** (*x\_dict={}*, *return\_dict=False*, *return\_all=True*, *\*\*kwargs*)

Evaluate the value of the loss function given inputs (*x\_dict*).

**Parameters**

- **x\_dict** (*dict*, defaults to *{}*) – Input variables.
- **return\_dict** (*bool*, default to *False*.) – Whether to return samples along with the evaluated value of the loss function.
- **return\_all** (*bool*, default to *True*.) – Whether to return all samples, including those that have not been updated.

**Returns**

- **loss** (*torch.Tensor*) – the evaluated value of the loss function.
- **x\_dict** (*dict*) – All samples generated when evaluating the loss function. If *return\_dict* is *False*, it is not returned.

**forward** (*x\_dict*, *\*\*kwargs*)

**Parameters** **x\_dict** (*dict*) – Input variables.

**Returns**

- a tuple of *pixyz.losses.Loss* and *dict*
- *deterministically calculated loss and updated all samples.*

## 2.2 Probability density function

### 2.2.1 LogProb

**class** *pixyz.losses.LogProb* (*p*, *sum\_features=True*, *feature\_dims=None*)

Bases: *pixyz.losses.losses.Loss*

The log probability density/mass function.

$$\log p(x)$$

## Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10])
>>> loss_cls = LogProb(p) # or p.log_prob()
>>> print(loss_cls)
\log p(x)
>>> sample_x = torch.randn(2, 10) # Psuedo data
>>> loss = loss_cls.eval({"x": sample_x})
>>> print(loss) # doctest: +SKIP
tensor([12.9894, 15.5280])
```

**forward** ( $x=\{\}$ , *\*\*kwargs*)

**Parameters** **x\_dict** (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and dict
- *deterministically calculrated loss and updated all samples.*

## 2.2.2 Prob

**class** `pixyz.losses.Prob` ( $p$ , *sum\_features=True*, *feature\_dims=None*)

Bases: `pixyz.losses.pdf.LogProb`

The probability density/mass function.

$$p(x) = \exp(\log p(x))$$

## Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10])
>>> loss_cls = Prob(p) # or p.prob()
>>> print(loss_cls)
p(x)
>>> sample_x = torch.randn(2, 10) # Psuedo data
>>> loss = loss_cls.eval({"x": sample_x})
>>> print(loss) # doctest: +SKIP
tensor([3.2903e-07, 5.5530e-07])
```

**forward** ( $x=\{\}$ , *\*\*kwargs*)

**Parameters** **x\_dict** (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and dict
- *deterministically calculrated loss and updated all samples.*



## 2.3 Expected value

### 2.3.1 Expectation

**class** pixyz.losses.**Expectation** (*p*, *f*, *sample\_shape*=torch.Size([1]), *reparam*=True)

Bases: `pixyz.losses.losses.Loss`

Expectation of a given function (Monte Carlo approximation).

$$\mathbb{E}_{p(x)}[f(x)] \approx \frac{1}{L} \sum_{l=1}^L f(x_l), \quad \text{where } x_l \sim p(x).$$

Note that  $f$  doesn't need to be able to sample, which is known as the law of the unconscious statistician (LOTUS).

Therefore, in this class,  $f$  is assumed to `pixyz.Loss`.

#### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal, Bernoulli
>>> from pixyz.losses import LogProb
>>> q = Normal(loc="x", scale=torch.tensor(1.), var=["z"], cond_var=["x"],
...           features_shape=[10]) # q(z/x)
>>> p = Normal(loc="z", scale=torch.tensor(1.), var=["x"], cond_var=["z"],
...           features_shape=[10]) # p(x/z)
>>> loss_cls = LogProb(p).expectation(q) # equals to Expectation(q, LogProb(p))
>>> print(loss_cls)
\mathbb{E}_{\{p(z|x)\}} \left[ \log p(x|z) \right]
>>> sample_x = torch.randn(2, 10) # Psuedo data
>>> loss = loss_cls.eval({"x": sample_x})
>>> print(loss) # doctest: +SKIP
tensor([-12.8181, -12.6062])
>>> loss_cls = LogProb(p).expectation(q, sample_shape=(5,))
>>> loss = loss_cls.eval({"x": sample_x})
>>> print(loss) # doctest: +SKIP
>>> q = Bernoulli(probs=torch.tensor(0.5), var=["x"], cond_var=[], features_
↪ shape=[10]) # q(x)
>>> p = Bernoulli(probs=torch.tensor(0.3), var=["x"], cond_var=[], features_
↪ shape=[10]) # p(x)
>>> loss_cls = p.log_prob().expectation(q, sample_shape=[64])
>>> train_loss = loss_cls.eval()
>>> print(train_loss) # doctest: +SKIP
tensor([46.7559])
>>> eval_loss = loss_cls.eval(test_mode=True)
>>> print(eval_loss) # doctest: +SKIP
tensor([-7.6047])
```

**forward** (*x\_dict*={}, \*\**kwargs*)

Parameters **x\_dict** (*dict*) – Input variables.

Returns

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calcularted loss and updated all samples.*

## 2.3.2 REINFORCE

`pixyz.losses.REINFORCE(p, f, b=0, sample_shape=torch.Size([1]), reparam=True)`

Surrogate Loss for Policy Gradient Method (REINFORCE) with a given reward function  $f$  and a given baseline  $b$ .

$$\mathbb{E}_{p(x)}[\text{detach}(f(x) - b(x)) \log p(x) + f(x) - b(x)].$$

in this function,  $f$  and  $b$  is assumed to `pixyz.Loss`.

### Parameters

- **p** (`pixyz.distributions.Distribution`) – Distribution for expectation.
- **f** (`pixyz.losses.Loss`) – reward function
- **b** (`pixyz.losses.Loss` default to `pixyz.losses.ValueLoss(0)`) – baseline function
- **sample\_shape** (`torch.Size` default to `torch.Size([1])`) – sample size for expectation
- **reparam** – using reparameterization in internal sampling

**Returns** `surrogate_loss` – policy gradient can be calculated from a gradient of this surrogate loss.

**Return type** `pixyz.losses.Loss`

### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal, Bernoulli
>>> from pixyz.losses import LogProb
>>> q = Bernoulli(probs=torch.tensor(0.5), var=["x"], cond_var=[], features_
↳shape=[10]) # q(x)
>>> p = Bernoulli(probs=torch.tensor(0.3), var=["x"], cond_var=[], features_
↳shape=[10]) # p(x)
>>> loss_cls = REINFORCE(q, p.log_prob(), sample_shape=[64])
>>> train_loss = loss_cls.eval(test_mode=True)
>>> print(train_loss) # doctest: +SKIP
tensor([46.7559])
>>> loss_cls = p.log_prob().expectation(q, sample_shape=[64])
>>> test_loss = loss_cls.eval()
>>> print(test_loss) # doctest: +SKIP
tensor([-7.6047])
```

## 2.4 Entropy

### 2.4.1 Entropy

`pixyz.losses.Entropy(p, analytical=True, sample_shape=torch.Size([1]))`

Entropy (Analytical or Monte Carlo approximation).

$$H(p) = -\mathbb{E}_{p(x)}[\log p(x)] \quad (\text{analytical})$$

$$\approx -\frac{1}{L} \sum_{l=1}^L \log p(x_l), \quad \text{where } x_l \sim p(x) \quad (\text{MC approximation}).$$

## Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"], features_
↳shape=[64])
>>> loss_cls = Entropy(p, analytical=True)
>>> print(loss_cls)
H \left[ \{p(x)\} \right]
>>> loss_cls.eval()
tensor([90.8121])
>>> loss_cls = Entropy(p, analytical=False, sample_shape=[10])
>>> print(loss_cls)
- \mathbb{E}_{\{p(x)\}} \left[ \log p(x) \right]
>>> loss_cls.eval() # doctest: +SKIP
tensor([90.5991])
```

## 2.4.2 CrossEntropy

`pixyz.losses.CrossEntropy(p, q, analytical=False, sample_shape=torch.Size([1]))`

Cross entropy, a.k.a., the negative expected value of log-likelihood (Monte Carlo approximation or Analytical).

$$H(p, q) = -\mathbb{E}_{p(x)}[\log q(x)] \quad (\text{analytical})$$

$$\approx -\frac{1}{L} \sum_{l=1}^L \log q(x_l), \quad \text{where } x_l \sim p(x) \quad (\text{MC approximation}).$$

## Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"], features_
↳shape=[64], name="p")
>>> q = Normal(loc=torch.tensor(1.), scale=torch.tensor(1.), var=["x"], features_
↳shape=[64], name="q")
>>> loss_cls = CrossEntropy(p, q, analytical=True)
>>> print(loss_cls)
D_{KL} \left[ p(x) || q(x) \right] + H \left[ \{p(x)\} \right]
>>> loss_cls.eval()
tensor([122.8121])
>>> loss_cls = CrossEntropy(p, q, analytical=False, sample_shape=[10])
>>> print(loss_cls)
- \mathbb{E}_{\{p(x)\}} \left[ \log q(x) \right]
>>> loss_cls.eval() # doctest: +SKIP
tensor([123.2192])
```

## 2.5 Lower bound

### 2.5.1 ELBO

`pixyz.losses.ELBO(p, q, sample_shape=torch.Size([1]))`

The evidence lower bound (Monte Carlo approximation).

$$\mathbb{E}_{q(z|x)} \left[ \log \frac{p(x, z)}{q(z|x)} \right] \approx \frac{1}{L} \sum_{l=1}^L \log p(x, z_l), \quad \text{where } z_l \sim q(z|x).$$

---

**Note:** This class is a special case of the *Expectation* class.

---

#### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> q = Normal(loc="x", scale=torch.tensor(1.), var=["z"], cond_var=["x"],
↳ features_shape=[64]) # q(z|x)
>>> p = Normal(loc="z", scale=torch.tensor(1.), var=["x"], cond_var=["z"],
↳ features_shape=[64]) # p(x/z)
>>> loss_cls = ELBO(p, q)
>>> print(loss_cls)
\mathbb{E}_{p(z|x)} \left[ \log p(x|z) - \log p(z|x) \right]
>>> loss = loss_cls.eval({"x": torch.randn(1, 64)})
```

## 2.6 Statistical distance

### 2.6.1 KullbackLeibler

`pixyz.losses.KullbackLeibler(p, q, dim=None, analytical=True, sample_shape=torch.Size([1]))`

Kullback-Leibler divergence (analytical or Monte Carlo Approximation).

$$D_{KL}[p||q] = \mathbb{E}_{p(x)} \left[ \log \frac{p(x)}{q(x)} \right] \quad (\text{analytical})$$

$$\approx \frac{1}{L} \sum_{l=1}^L \log \frac{p(x_l)}{q(x_l)}, \quad \text{where } x_l \sim p(x) \quad (\text{MC approximation}).$$

#### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal, Beta
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["z"], features_
↳ shape=[64], name="p")
>>> q = Normal(loc=torch.tensor(1.), scale=torch.tensor(1.), var=["z"], features_
↳ shape=[64], name="q")
>>> loss_cls = KullbackLeibler(p, q, analytical=True)
```

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```

>>> print(loss_cls)
D_{KL} \left[p(z)||q(z) \right]
>>> loss_cls.eval()
tensor([32.])
>>> loss_cls = KullbackLeibler(p,q,analytical=False,sample_shape=[64])
>>> print(loss_cls)
\mathbb{E}_{p(z)} \left[\log p(z) - \log q(z) \right]
>>> loss_cls.eval() # doctest: +SKIP
tensor([31.4713])

```

## 2.6.2 WassersteinDistance

**class** pixyz.losses.WassersteinDistance(*p, q, metric=PairwiseDistance()*)

Bases: pixyz.losses.losses.Divergence

Wasserstein distance.

$$W(p, q) = \inf_{\Gamma \in \mathcal{P}(x_p \sim p, x_q \sim q)} \mathbb{E}_{(x_p, x_q) \sim \Gamma} [d(x_p, x_q)]$$

However, instead of the above true distance, this class computes the following one.

$$W'(p, q) = \mathbb{E}_{x_p \sim p, x_q \sim q} [d(x_p, x_q)].$$

Here,  $W'$  is the upper of  $W$  (i.e.,  $W \leq W'$ ), and these are equal when both  $p$  and  $q$  are degenerate (deterministic) distributions.

### Examples

```

>>> import torch
>>> from pixyz.distributions import Normal
>>> p = Normal(loc="x", scale=torch.tensor(1.), var=["z"], cond_var=["x"],
↳ features_shape=[64], name="p")
>>> q = Normal(loc="x", scale=torch.tensor(1.), var=["z"], cond_var=["x"],
↳ features_shape=[64], name="q")
>>> loss_cls = WassersteinDistance(p, q)
>>> print(loss_cls)
W^{upper} \left(p(z|x), q(z|x) \right)
>>> loss = loss_cls.eval({"x": torch.randn(1, 64)})

```

**forward**(*x\_dict, \*\*kwargs*)

**Parameters** *x\_dict* (*dict*) – Input variables.

**Returns**

- a tuple of pixyz.losses.Loss and dict
- *deterministically calculrated loss and updated all samples.*

## 2.6.3 MMD

**class** pixyz.losses.MMD(*p, q, kernel='gaussian', \*\*kernel\_params*)

Bases: pixyz.losses.losses.Divergence

The Maximum Mean Discrepancy (MMD).

$$D_{MMD^2}[p||q] = \mathbb{E}_{p(x),p(x')}[k(x,x')] + \mathbb{E}_{q(x),q(x')}[k(x,x')] - 2\mathbb{E}_{p(x),q(x')}[k(x,x')]$$

where  $k(x, x')$  is any positive definite kernel.

## Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> p = Normal(loc="x", scale=torch.tensor(1.), var=["z"], cond_var=["x"],
↳features_shape=[64], name="p")
>>> q = Normal(loc="x", scale=torch.tensor(1.), var=["z"], cond_var=["x"],
↳features_shape=[64], name="q")
>>> loss_cls = MMD(p, q, kernel="gaussian")
>>> print(loss_cls)
D_{MMD^2} \left[p(z|x) || q(z|x) \right]
>>> loss = loss_cls.eval({"x": torch.randn(1, 64)})
>>> # Use the inverse (multi-)quadric kernel
>>> loss = MMD(p, q, kernel="inv-multiquadric").eval({"x": torch.randn(10, 64)})
```

**forward** ( $x\_dict=\{\}$ ,  $**kwargs$ )

**Parameters**  $x\_dict$  ( $dict$ ) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculated loss and updated all samples.*

## 2.7 Adversarial statistical distance

### 2.7.1 AdversarialJensenShannon

```
class pixyz.losses.AdversarialJensenShannon(p, q, discriminator, optimizer=<class
    'torch.optim.adam.Adam'>, optimizer_params={}, inverse_g_loss=True)
```

Bases: `pixyz.losses.adversarial_loss.AdversarialLoss`

Jensen-Shannon divergence (adversarial training).

$$D_{JS}[p(x)||q(x)] \leq 2 \cdot D_{JS}[p(x)||q(x)] + 2 \log 2 = \mathbb{E}_{p(x)}[\log d^*(x)] + \mathbb{E}_{q(x)}[\log(1 - d^*(x))],$$

where  $d^*(x) = \arg \max_d \mathbb{E}_{p(x)}[\log d(x)] + \mathbb{E}_{q(x)}[\log(1 - d(x))]$ .

This class acts as a metric that evaluates a given distribution (generator). If you want to learn this evaluation metric itself, i.e., discriminator (critic), use the `train` method.

## Examples

```

>>> import torch
>>> from pixyz.distributions import Deterministic, EmpiricalDistribution, Normal
>>> # Generator
>>> class Generator(Deterministic):
...     def __init__(self):
...         super(Generator, self).__init__(var=["x"], cond_var=["z"], name="p")
...         self.model = nn.Linear(32, 64)
...     def forward(self, z):
...         return {"x": self.model(z)}
>>> p_g = Generator()
>>> prior = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.),
...                 var=["z"], features_shape=[32], name="p_{prior}")
>>> p = (p_g*prior).marginalize_var("z")
>>> print(p)
Distribution:
  p(x) = \int p(x|z)p_{prior}(z)dz
Network architecture:
  p_{prior}(z):
  Normal(
    name=p_{prior}, distribution_name=Normal,
    var=['z'], cond_var=[], input_var=[], features_shape=torch.Size([32])
    (loc): torch.Size([1, 32])
    (scale): torch.Size([1, 32])
  )
  p(x|z):
  Generator(
    name=p, distribution_name=Deterministic,
    var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
    (model): Linear(in_features=32, out_features=64, bias=True)
  )
>>> # Data distribution (dummy distribution)
>>> p_data = EmpiricalDistribution(["x"])
>>> print(p_data)
Distribution:
  p_{data}(x)
Network architecture:
  EmpiricalDistribution(
    name=p_{data}, distribution_name=Data distribution,
    var=['x'], cond_var=[], input_var=['x'], features_shape=torch.Size([])
  )
>>> # Discriminator (critic)
>>> class Discriminator(Deterministic):
...     def __init__(self):
...         super(Discriminator, self).__init__(var=["t"], cond_var=["x"], name="d")
...         self.model = nn.Linear(64, 1)
...     def forward(self, x):
...         return {"t": torch.sigmoid(self.model(x))}
>>> d = Discriminator()
>>> print(d)
Distribution:
  d(t|x)
Network architecture:
  Discriminator(
    name=d, distribution_name=Deterministic,
    var=['t'], cond_var=['x'], input_var=['x'], features_shape=torch.Size([])
    (model): Linear(in_features=64, out_features=1, bias=True)

```

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```

    )
>>>
>>> # Set the loss class
>>> loss_cls = AdversarialJensenShannon(p, p_data, discriminator=d)
>>> print(loss_cls)
mean(D_{JS}^{\text{Adv}} \left[p(x) || p_{\text{data}}(x) \right])
>>>
>>> sample_x = torch.randn(2, 64) # Psuedo data
>>> loss = loss_cls.eval({"x": sample_x})
>>> print(loss) # doctest: +SKIP
tensor(1.3723, grad_fn=<AddBackward0>)
>>> # For evaluating a discriminator loss, set the `discriminator` option to True.
>>> loss_d = loss_cls.eval({"x": sample_x}, discriminator=True)
>>> print(loss_d) # doctest: +SKIP
tensor(1.4990, grad_fn=<AddBackward0>)
>>> # When training the evaluation metric (discriminator), use the train method.
>>> train_loss = loss_cls.loss_train({"x": sample_x})

```

## References

[Goodfellow+ 2014] Generative Adversarial Networks

**forward** (*x\_dict*, *discriminator=False*, *\*\*kwargs*)

**Parameters** *x\_dict* (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

**d\_loss** (*y\_p*, *y\_q*, *batch\_n*)

Evaluate a discriminator loss given outputs of the discriminator.

**Parameters**

- *y\_p* (*torch.Tensor*) – Output of discriminator given sample from p.
- *y\_q* (*torch.Tensor*) – Output of discriminator given sample from q.
- *batch\_n* (*int*) – Batch size of inputs.

**Returns**

**Return type** `torch.Tensor`

**g\_loss** (*y\_p*, *y\_q*, *batch\_n*)

Evaluate a generator loss given outputs of the discriminator.

**Parameters**

- *y\_p* (*torch.Tensor*) – Output of discriminator given sample from p.
- *y\_q* (*torch.Tensor*) – Output of discriminator given sample from q.
- *batch\_n* (*int*) – Batch size of inputs.

**Returns**

**Return type** `torch.Tensor`



**loss\_train** (*train\_x\_dict*, *\*\*kwargs*)  
Train the evaluation metric (discriminator).

**Parameters**

- **train\_x\_dict** (*dict*) – Input variables.
- **\*\*kwargs** – Arbitrary keyword arguments.

**Returns loss**

**Return type** torch.Tensor

**loss\_test** (*test\_x\_dict*, *\*\*kwargs*)  
Test the evaluation metric (discriminator).

**Parameters**

- **test\_x\_dict** (*dict*) – Input variables.
- **\*\*kwargs** – Arbitrary keyword arguments.

**Returns loss**

**Return type** torch.Tensor

## 2.7.2 AdversarialKullbackLeibler

**class** pixyz.losses.**AdversarialKullbackLeibler** (*p*, *q*, *discriminator*, *\*\*kwargs*)  
Bases: pixyz.losses.adversarial\_loss.AdversarialLoss

Kullback-Leibler divergence (adversarial training).

$$D_{KL}[p(x)||q(x)] = \mathbb{E}_{p(x)} \left[ \log \frac{p(x)}{q(x)} \right] \approx \mathbb{E}_{p(x)} \left[ \log \frac{d^*(x)}{1 - d^*(x)} \right],$$

where  $d^*(x) = \arg \max_d \mathbb{E}_{q(x)}[\log d(x)] + \mathbb{E}_{p(x)}[\log(1 - d(x))]$ .

Note that this divergence is minimized to close  $p$  to  $q$ .

### Examples

```
>>> import torch
>>> from pixyz.distributions import Deterministic, EmpiricalDistribution, Normal
>>> # Generator
>>> class Generator(Deterministic):
...     def __init__(self):
...         super(Generator, self).__init__(var=["x"], cond_var=["z"], name="p")
...         self.model = nn.Linear(32, 64)
...     def forward(self, z):
...         return {"x": self.model(z)}
>>> p_g = Generator()
>>> prior = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.),
...                 var=["z"], features_shape=[32], name="p_{prior}")
>>> p = (p_g*prior).marginalize_var("z")
>>> print(p)
Distribution:
  p(x) = \int p(x|z)p_{prior}(z)dz
Network architecture:
  p_{prior}(z):
```

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```

Normal(
  name=p_{prior}, distribution_name=Normal,
  var=['z'], cond_var=[], input_var=[], features_shape=torch.Size([32])
  (loc): torch.Size([1, 32])
  (scale): torch.Size([1, 32])
)
p(x|z):
Generator(
  name=p, distribution_name=Deterministic,
  var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
  (model): Linear(in_features=32, out_features=64, bias=True)
)
>>> # Data distribution (dummy distribution)
>>> p_data = EmpiricalDistribution(["x"])
>>> print(p_data)
Distribution:
  p_{data}(x)
Network architecture:
  EmpiricalDistribution(
    name=p_{data}, distribution_name=Data distribution,
    var=['x'], cond_var=[], input_var=['x'], features_shape=torch.Size([])
  )
>>> # Discriminator (critic)
>>> class Discriminator(Deterministic):
...     def __init__(self):
...         super(Discriminator, self).__init__(var=["t"], cond_var=["x"], name="d
↳")
...         self.model = nn.Linear(64, 1)
...     def forward(self, x):
...         return {"t": torch.sigmoid(self.model(x))}
>>> d = Discriminator()
>>> print(d)
Distribution:
  d(t|x)
Network architecture:
  Discriminator(
    name=d, distribution_name=Deterministic,
    var=['t'], cond_var=['x'], input_var=['x'], features_shape=torch.Size([])
    (model): Linear(in_features=64, out_features=1, bias=True)
  )
>>>
>>> # Set the loss class
>>> loss_cls = AdversarialKullbackLeibler(p, p_data, discriminator=d)
>>> print(loss_cls)
mean(D_{KL}^{\text{Adv}} \left[ p(x) || p_{\text{data}}(x) \right])
>>>
>>> sample_x = torch.randn(2, 64) # Psuedo data
>>> loss = loss_cls.eval({"x": sample_x})
>>> # The evaluation value might be negative if the discriminator training is
↳incomplete.
>>> print(loss) # doctest: +SKIP
tensor(-0.8377, grad_fn=<AddBackward0>)
>>> # For evaluating a discriminator loss, set the `discriminator` option to True.
>>> loss_d = loss_cls.eval({"x": sample_x}, discriminator=True)
>>> print(loss_d) # doctest: +SKIP
tensor(1.9321, grad_fn=<AddBackward0>)
>>> # When training the evaluation metric (discriminator), use the train method.

```

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```
>>> train_loss = loss_cls.loss_train({"x": sample_x})
```

## References

[Kim+ 2018] Disentangling by Factorising

**forward** (*x\_dict*, *discriminator=False*, *\*\*kwargs*)

**Parameters** *x\_dict* (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

**g\_loss** (*y\_p*, *batch\_n*)

Evaluate a generator loss given an output of the discriminator.

**Parameters**

- *y\_p* (*torch.Tensor*) – Output of discriminator given sample from p.
- *batch\_n* (*int*) – Batch size of inputs.

**Returns**

**Return type** `torch.Tensor`

**d\_loss** (*y\_p*, *y\_q*, *batch\_n*)

Evaluate a discriminator loss given outputs of the discriminator.

**Parameters**

- *y\_p* (*torch.Tensor*) – Output of discriminator given sample from p.
- *y\_q* (*torch.Tensor*) – Output of discriminator given sample from q.
- *batch\_n* (*int*) – Batch size of inputs.

**Returns**

**Return type** `torch.Tensor`

**loss\_train** (*train\_x\_dict*, *\*\*kwargs*)

Train the evaluation metric (discriminator).

**Parameters**

- *train\_x\_dict* (*dict*) – Input variables.
- *\*\*kwargs* – Arbitrary keyword arguments.

**Returns** `loss`

**Return type** `torch.Tensor`

**loss\_test** (*test\_x\_dict*, *\*\*kwargs*)

Test the evaluation metric (discriminator).

**Parameters**

- *test\_x\_dict* (*dict*) – Input variables.
- *\*\*kwargs* – Arbitrary keyword arguments.

**Returns** loss**Return type** torch.Tensor

### 2.7.3 AdversarialWassersteinDistance

**class** pixyz.losses.**AdversarialWassersteinDistance** (*p*, *q*, *discriminator*,  
*clip\_value=0.01*, *\*\*kwargs*)

Bases: pixyz.losses.adversarial\_loss.AdversarialJensenShannon

Wasserstein distance (adversarial training).

$$W(p, q) = \sup_{||d||_L \leq 1} \mathbb{E}_{p(x)}[d(x)] - \mathbb{E}_{q(x)}[d(x)]$$

#### Examples

```
>>> import torch
>>> from pixyz.distributions import Deterministic, EmpiricalDistribution, Normal
>>> # Generator
>>> class Generator(Deterministic):
...     def __init__(self):
...         super(Generator, self).__init__(var=["x"], cond_var=["z"], name="p")
...         self.model = nn.Linear(32, 64)
...     def forward(self, z):
...         return {"x": self.model(z)}
>>> p_g = Generator()
>>> prior = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.),
...                 var=["z"], features_shape=[32], name="p_{prior}")
>>> p = (p_g*prior).marginalize_var("z")
>>> print(p)
Distribution:
p(x) = \int p(x|z)p_{prior}(z)dz
Network architecture:
p_{prior}(z):
Normal(
  name=p_{prior}, distribution_name=Normal,
  var=['z'], cond_var=[], input_var=[], features_shape=torch.Size([32])
  (loc): torch.Size([1, 32])
  (scale): torch.Size([1, 32])
)
p(x|z):
Generator(
  name=p, distribution_name=Deterministic,
  var=['x'], cond_var=['z'], input_var=['z'], features_shape=torch.Size([])
  (model): Linear(in_features=32, out_features=64, bias=True)
)
>>> # Data distribution (dummy distribution)
>>> p_data = EmpiricalDistribution(["x"])
>>> print(p_data)
Distribution:
p_{data}(x)
Network architecture:
EmpiricalDistribution(
  name=p_{data}, distribution_name=Data distribution,
  var=['x'], cond_var=[], input_var=['x'], features_shape=torch.Size([])
```

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```

)
>>> # Discriminator (critic)
>>> class Discriminator(Deterministic):
...     def __init__(self):
...         super(Discriminator, self).__init__(var=["t"], cond_var=["x"], name="d
↪")
...         self.model = nn.Linear(64, 1)
...     def forward(self, x):
...         return {"t": self.model(x)}
>>> d = Discriminator()
>>> print(d)
Distribution:
  d(t|x)
Network architecture:
  Discriminator(
    name=d, distribution_name=Deterministic,
    var=['t'], cond_var=['x'], input_var=['x'], features_shape=torch.Size([])
    (model): Linear(in_features=64, out_features=1, bias=True)
  )
>>>
>>> # Set the loss class
>>> loss_cls = AdversarialWassersteinDistance(p, p_data, discriminator=d)
>>> print(loss_cls)
mean(W^{Adv} \left(p(x), p_{data}(x) \right))
>>>
>>> sample_x = torch.randn(2, 64) # Psuedo data
>>> loss = loss_cls.eval({"x": sample_x})
>>> print(loss) # doctest: +SKIP
tensor(-0.0060, grad_fn=<SubBackward0>)
>>> # For evaluating a discriminator loss, set the `discriminator` option to True.
>>> loss_d = loss_cls.eval({"x": sample_x}, discriminator=True)
>>> print(loss_d) # doctest: +SKIP
tensor(-0.3802, grad_fn=<NegBackward>)
>>> # When training the evaluation metric (discriminator), use the train method.
>>> train_loss = loss_cls.loss_train({"x": sample_x})

```

## References

[Arjovsky+ 2017] Wasserstein GAN

**d\_loss** (*y\_p*, *y\_q*, \*args, \*\*kwargs)

Evaluate a discriminator loss given outputs of the discriminator.

### Parameters

- **y\_p** (*torch.Tensor*) – Output of discriminator given sample from p.
- **y\_q** (*torch.Tensor*) – Output of discriminator given sample from q.
- **batch\_n** (*int*) – Batch size of inputs.

### Returns

**Return type** torch.Tensor

**g\_loss** (*y\_p*, *y\_q*, \*args, \*\*kwargs)

Evaluate a generator loss given outputs of the discriminator.

### Parameters

- **y\_p** (*torch.Tensor*) – Output of discriminator given sample from p.
- **y\_q** (*torch.Tensor*) – Output of discriminator given sample from q.
- **batch\_n** (*int*) – Batch size of inputs.

**Returns****Return type** torch.Tensor**loss\_train** (*train\_x\_dict*, *\*\*kwargs*)

Train the evaluation metric (discriminator).

**Parameters**

- **train\_x\_dict** (*dict*) – Input variables.
- **\*\*kwargs** – Arbitrary keyword arguments.

**Returns loss****Return type** torch.Tensor**loss\_test** (*test\_x\_dict*, *\*\*kwargs*)

Test the evaluation metric (discriminator).

**Parameters**

- **test\_x\_dict** (*dict*) – Input variables.
- **\*\*kwargs** – Arbitrary keyword arguments.

**Returns loss****Return type** torch.Tensor

## 2.8 Loss for sequential distributions

### 2.8.1 IterativeLoss

```
class pixyz.losses.IterativeLoss (step_loss, max_iter=None, series_var=(), update_value={},  
                                  slice_step=None, timestep_var=())
```

Bases: `pixyz.losses.losses.Loss`

Iterative loss.

This class allows implementing an arbitrary model which requires iteration.

$$\mathcal{L} = \sum_{t=0}^{T-1} \mathcal{L}_{step}(x_t, h_t),$$

where  $x_t = f_{slice\_step}(x, t)$ .**Examples**

```
>>> import torch
>>> from torch.nn import functional as F
>>> from pixyz.distributions import Normal, Bernoulli, Deterministic
>>>
>>> # Set distributions
```

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```

>>> x_dim = 128
>>> z_dim = 64
>>> h_dim = 32
>>>
>>> #  $p(x|z, h_{\text{prev}})$ 
>>> class Decoder(Bernoulli):
...     def __init__(self):
...         super().__init__(var=["x"], cond_var=["z", "h_prev"], name="p")
...         self.fc = torch.nn.Linear(z_dim + h_dim, x_dim)
...     def forward(self, z, h_prev):
...         return {"probs": torch.sigmoid(self.fc(torch.cat((z, h_prev), dim=-
↪1)))}
...
>>> #  $q(z|x, h_{\text{prev}})$ 
>>> class Encoder(Normal):
...     def __init__(self):
...         super().__init__(var=["z"], cond_var=["x", "h_prev"], name="q")
...         self.fc_loc = torch.nn.Linear(x_dim + h_dim, z_dim)
...         self.fc_scale = torch.nn.Linear(x_dim + h_dim, z_dim)
...     def forward(self, x, h_prev):
...         xh = torch.cat((x, h_prev), dim=-1)
...         return {"loc": self.fc_loc(xh), "scale": F.softplus(self.fc_
↪scale(xh))}
...
>>> #  $f(h|x, z, h_{\text{prev}})$  (update h)
>>> class Recurrence(Deterministic):
...     def __init__(self):
...         super().__init__(var=["h"], cond_var=["x", "z", "h_prev"], name="f")
...         self.rnn_cell = torch.nn.GRUCell(x_dim + z_dim, h_dim)
...     def forward(self, x, z, h_prev):
...         return {"h": self.rnn_cell(torch.cat((z, x), dim=-1), h_prev)}
>>>
>>> p = Decoder()
>>> q = Encoder()
>>> f = Recurrence()
>>>
>>> # Set the loss class
>>> step_loss_cls = p.log_prob().expectation(q * f).mean()
>>> print(step_loss_cls)
mean \left(\mathbb{E}_{q(z, h|x, h_{\text{prev}})} \left[ \log p(x|z, h_{\text{prev}}) \right] \right)
↪
>>> loss_cls = IterativeLoss(step_loss=step_loss_cls,
...                           series_var=["x"], update_value={"h": "h_prev"})
>>> print(loss_cls)
\sum_{t=0}^{t_{\text{max}} - 1} \text{mean} \left[ \mathbb{E}_{q(z, h|x, h_{\text{prev}})} \left[ \log \right. \right.
↪ \left. \left. p(x|z, h_{\text{prev}}) \right] \right]
>>>
>>> # Evaluate
>>> x_sample = torch.randn(30, 2, 128) # (timestep_size, batch_size, feature_size)
>>> h_init = torch.zeros(2, 32) # (batch_size, h_dim)
>>> loss = loss_cls.eval({"x": x_sample, "h_prev": h_init})
>>> print(loss) # doctest: +SKIP
tensor(-2826.0906, grad_fn=<AddBackward0>

```

**slice\_step\_fn**(*t*, *x*)

**forward**(*x\_dict*, *\*\*kwargs*)

**Parameters** `x_dict` (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and dict
- *deterministically calculated loss and updated all samples.*

## 2.9 Loss for special purpose

### 2.9.1 Parameter

**class** `pixyz.losses.losses.Parameter` (*input\_var*)

Bases: `pixyz.losses.losses.Loss`

This class defines a single variable as a loss class.

It can be used such as a coefficient parameter of a loss class.

#### Examples

```
>>> loss_cls = Parameter("x")
>>> print(loss_cls)
x
>>> loss = loss_cls.eval({"x": 2})
>>> print(loss)
2
```

**forward** (*x\_dict*=`{}`, *\*\*kwargs*)

**Parameters** `x_dict` (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and dict
- *deterministically calculated loss and updated all samples.*

### 2.9.2 ValueLoss

**class** `pixyz.losses.losses.ValueLoss` (*loss1*)

Bases: `pixyz.losses.losses.Loss`

This class contains a scalar as a loss value.

If multiplying a scalar by an arbitrary loss class, this scalar is converted to the `ValueLoss`.

#### Examples

```
>>> loss_cls = ValueLoss(2)
>>> print(loss_cls)
2
>>> loss = loss_cls.eval()
>>> print(loss)
tensor(2.)
```



**forward** (*x\_dict*={}, \*\**kwargs*)

Parameters **x\_dict** (*dict*) – Input variables.

Returns

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.9.3 ConstantVar

**class** `pixyz.losses.losses.ConstantVar` (*base\_loss*, *constant\_dict*)

Bases: `pixyz.losses.losses.Loss`

This class is defined as a loss class that makes the value of a variable a constant before evaluation.

It can be used to fix the coefficient parameters of the loss class or to condition random variables.

### Examples

```
>>> loss_cls = Parameter('x').constant_var({'x': 1})
>>> print(loss_cls)
x
>>> loss = loss_cls.eval()
>>> print(loss)
1
```

**forward** (*x\_dict*={}, \*\**kwargs*)

Parameters **x\_dict** (*dict*) – Input variables.

Returns

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.10 Operators

### 2.10.1 LossOperator

**class** `pixyz.losses.losses.LossOperator` (*loss1*, *loss2*)

Bases: `pixyz.losses.losses.Loss`

**forward** (*x\_dict*={}, \*\**kwargs*)

Parameters **x\_dict** (*dict*) – Input variables.

Returns

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.10.2 LossSelfOperator

```
class pixyz.losses.losses.LossSelfOperator (loss1)
    Bases: pixyz.losses.losses.Loss

    loss_train (x_dict={}, **kwargs)

    loss_test (x_dict={}, **kwargs)
```

## 2.10.3 AddLoss

```
class pixyz.losses.losses.AddLoss (loss1, loss2)
    Bases: pixyz.losses.losses.LossOperator

    Apply the add operation to the two losses.
```

### Examples

```
>>> loss_cls_1 = ValueLoss(2)
>>> loss_cls_2 = Parameter("x")
>>> loss_cls = loss_cls_1 + loss_cls_2  # equals to AddLoss(loss_cls_1, loss_cls_
↪2)
>>> print(loss_cls)
x + 2
>>> loss = loss_cls.eval({"x": 3})
>>> print(loss)
tensor(5.)
```

```
forward (x_dict={}, **kwargs)
```

**Parameters** **x\_dict** (*dict*) – Input variables.

### Returns

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.10.4 SubLoss

```
class pixyz.losses.losses.SubLoss (loss1, loss2)
    Bases: pixyz.losses.losses.LossOperator

    Apply the sub operation to the two losses.
```

### Examples

```
>>> loss_cls_1 = ValueLoss(2)
>>> loss_cls_2 = Parameter("x")
>>> loss_cls = loss_cls_1 - loss_cls_2  # equals to SubLoss(loss_cls_1, loss_cls_
↪2)
>>> print(loss_cls)
2 - x
>>> loss = loss_cls.eval({"x": 4})
>>> print(loss)
```

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```

tensor(-2.)
>>> loss_cls = loss_cls_2 - loss_cls_1 # equals to SubLoss(loss_cls_2, loss_cls_
↪1)
>>> print(loss_cls)
x - 2
>>> loss = loss_cls.eval({"x": 4})
>>> print(loss)
tensor(2.)

```

**forward** ( $x\_dict=\{\}$ , *\*\*kwargs*)

**Parameters** **x\_dict** (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculatred loss and updated all samples.*

### 2.10.5 MulLoss

**class** `pixyz.losses.losses.MulLoss` (*loss1, loss2*)

Bases: `pixyz.losses.losses.LossOperator`

Apply the *mul* operation to the two losses.

#### Examples

```

>>> loss_cls_1 = ValueLoss(2)
>>> loss_cls_2 = Parameter("x")
>>> loss_cls = loss_cls_1 * loss_cls_2 # equals to MulLoss(loss_cls_1, loss_cls_
↪2)
>>> print(loss_cls)
2 x
>>> loss = loss_cls.eval({"x": 4})
>>> print(loss)
tensor(8.)

```

**forward** ( $x\_dict=\{\}$ , *\*\*kwargs*)

**Parameters** **x\_dict** (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculatred loss and updated all samples.*

### 2.10.6 DivLoss

**class** `pixyz.losses.losses.DivLoss` (*loss1, loss2*)

Bases: `pixyz.losses.losses.LossOperator`

Apply the *div* operation to the two losses.

## Examples

```
>>> loss_cls_1 = ValueLoss(2)
>>> loss_cls_2 = Parameter("x")
>>> loss_cls = loss_cls_1 / loss_cls_2 # equals to DivLoss(loss_cls_1, loss_cls_
↪2)
>>> print(loss_cls)
\frac{2}{x}
>>> loss = loss_cls.eval({"x": 4})
>>> print(loss)
tensor(0.5000)
>>> loss_cls = loss_cls_2 / loss_cls_1 # equals to DivLoss(loss_cls_2, loss_cls_
↪1)
>>> print(loss_cls)
\frac{x}{2}
>>> loss = loss_cls.eval({"x": 4})
>>> print(loss)
tensor(2.)
```

**forward** (*x\_dict*={}, \*\*kwargs)

Parameters **x\_dict** (*dict*) – Input variables.

Returns

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.10.7 MinLoss

**class** `pixyz.losses.losses.MinLoss` (*loss1*, *loss2*)

Bases: `pixyz.losses.losses.LossOperator`

Apply the *min* operation to the loss.

## Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> from pixyz.losses.losses import ValueLoss, Parameter, MinLoss
>>> loss_min= MinLoss(ValueLoss(3), ValueLoss(1))
>>> print(loss_min)
min \left(3, 1\right)
>>> print(loss_min.eval())
tensor(1.)
```

**forward** (*x\_dict*={}, \*\*kwargs)

Parameters **x\_dict** (*dict*) – Input variables.

Returns

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.10.8 MaxLoss

**class** pixyz.losses.losses.**MaxLoss** (*loss1, loss2*)

Bases: *pixyz.losses.losses.LossOperator*

Apply the *max* operation to the loss.

### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> from pixyz.losses.losses import ValueLoss, MaxLoss
>>> loss_max= MaxLoss(ValueLoss(3), ValueLoss(1))
>>> print(loss_max)
max \left(3, 1\right)
>>> print(loss_max.eval())
tensor(3.)
```

**forward** (*x\_dict={}*, *\*\*kwargs*)

Parameters **x\_dict** (*dict*) – Input variables.

Returns

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.10.9 NegLoss

**class** pixyz.losses.losses.**NegLoss** (*loss1*)

Bases: *pixyz.losses.losses.LossSelfOperator*

Apply the *neg* operation to the loss.

### Examples

```
>>> loss_cls_1 = Parameter("x")
>>> loss_cls = -loss_cls_1 # equals to NegLoss(loss_cls_1)
>>> print(loss_cls)
- x
>>> loss = loss_cls.eval({"x": 4})
>>> print(loss)
-4
```

**forward** (*x\_dict={}*, *\*\*kwargs*)

Parameters **x\_dict** (*dict*) – Input variables.

Returns

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.10.10 AbsLoss

**class** pixyz.losses.losses.**AbsLoss** (*lossl*)  
 Bases: *pixyz.losses.losses.LossSelfOperator*

Apply the *abs* operation to the loss.

### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> from pixyz.losses import LogProb
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10])
>>> loss_cls = LogProb(p).abs() # equals to AbsLoss(LogProb(p))
>>> print(loss_cls)
|\log p(x)|
>>> sample_x = torch.randn(2, 10) # Psuedo data
>>> loss = loss_cls.eval({"x": sample_x})
>>> print(loss) # doctest: +SKIP
tensor([12.9894, 15.5280])
```

**forward** (*x\_dict*={}, \*\**kwargs*)

**Parameters** *x\_dict* (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.10.11 BatchMean

**class** pixyz.losses.losses.**BatchMean** (*lossl*)  
 Bases: *pixyz.losses.losses.LossSelfOperator*

Average a loss class over given batch data.

$$\mathbb{E}_{p_{data}(x)}[\mathcal{L}(x)] \approx \frac{1}{N} \sum_{i=1}^N \mathcal{L}(x_i),$$

where  $x_i \sim p_{data}(x)$  and  $\mathcal{L}$  is a loss function.

### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> from pixyz.losses import LogProb
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10])
>>> loss_cls = LogProb(p).mean() # equals to BatchMean(LogProb(p))
>>> print(loss_cls)
mean \left(\log p(x) \right)
>>> sample_x = torch.randn(2, 10) # Psuedo data
```

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```
>>> loss = loss_cls.eval({"x": sample_x})
>>> print(loss) # doctest: +SKIP
tensor(-14.5038)
```

**forward** (*x\_dict*={}, \*\*kwargs)

**Parameters** *x\_dict* (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.10.12 BatchSum

**class** `pixyz.losses.losses.BatchSum` (*lossl*)

Bases: `pixyz.losses.losses.LossSelfOperator`

Summation a loss class over given batch data.

$$\sum_{i=1}^N \mathcal{L}(x_i),$$

where  $x_i \sim p_{data}(x)$  and  $\mathcal{L}$  is a loss function.

### Examples

```
>>> import torch
>>> from pixyz.distributions import Normal
>>> from pixyz.losses import LogProb
>>> p = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.), var=["x"],
...           features_shape=[10])
>>> loss_cls = LogProb(p).sum() # equals to BatchSum(LogProb(p))
>>> print(loss_cls)
sum \left(\log p(x) \right)
>>> sample_x = torch.randn(2, 10) # Psuedo data
>>> loss = loss_cls.eval({"x": sample_x})
>>> print(loss) # doctest: +SKIP
tensor(-31.9434)
```

**forward** (*x\_dict*={}, \*\*kwargs)

**Parameters** *x\_dict* (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*

## 2.10.13 Detach

**class** `pixyz.losses.losses.Detach` (*lossl*)

Bases: `pixyz.losses.losses.LossSelfOperator`

Apply the *detach* method to the loss.

**forward** (*x\_dict*={}, *\*\*kwargs*)

Parameters **x\_dict** (*dict*) – Input variables.

Returns

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculated loss and updated all samples.*

## 2.10.14 DataParalleledLoss

**class** `pixyz.losses.losses.DataParalleledLoss` (*loss*, *distributed=False*, *\*\*kwargs*)

Bases: `pixyz.losses.losses.Loss`

Loss class wrapper of `torch.nn.DataParallel`. It can be used as the original loss class. *eval* & *forward* methods support data-parallel running.

### Examples

```
>>> import torch
>>> from torch import optim
>>> from torch.nn import functional as F
>>> from pixyz.distributions import Bernoulli, Normal
>>> from pixyz.losses import KullbackLeibler, DataParalleledLoss
>>> from pixyz.models import Model
>>> used_gpu_i = set()
>>> used_gpu_g = set()
>>> # Set distributions (Distribution API)
>>> class Inference(Normal):
...     def __init__(self):
...         super().__init__(var=["z"], cond_var=["x"], name="q")
...         self.model_loc = torch.nn.Linear(128, 64)
...         self.model_scale = torch.nn.Linear(128, 64)
...     def forward(self, x):
...         used_gpu_i.add(x.device.index)
...         return {"loc": self.model_loc(x), "scale": F.softplus(self.model_
↪scale(x))}
>>> class Generator(Bernoulli):
...     def __init__(self):
...         super().__init__(var=["x"], cond_var=["z"], name="p")
...         self.model = torch.nn.Linear(64, 128)
...     def forward(self, z):
...         used_gpu_g.add(z.device.index)
...         return {"probs": torch.sigmoid(self.model(z))}
>>> p = Generator()
>>> q = Inference()
>>> prior = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.),
...                 var=["z"], features_shape=[64], name="p_{prior}")
>>> # Define a loss function (Loss API)
>>> reconst = -p.log_prob().expectation(q)
>>> kl = KullbackLeibler(q, prior)
>>> batch_loss_cls = (reconst - kl)
>>> # device settings
>>> device = torch.device("cuda:0" if torch.cuda.is_available() else "cpu")
>>> device_count = torch.cuda.device_count()
>>> if device_count > 1:
```

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```

...     loss_cls = DataParalleledLoss(batch_loss_cls).mean().to(device)
... else:
...     loss_cls = batch_loss_cls.mean().to(device)
>>> # Set a model (Model API)
>>> model = Model(loss=loss_cls, distributions=[p, q],
...               optimizer=optim.Adam, optimizer_params={"lr": 1e-3})
>>> # Train and test the model
>>> data = torch.randn(2, 128).to(device) # Pseudo data
>>> train_loss = model.train({"x": data})
>>> expected = set(range(device_count)) if torch.cuda.is_available() else {None}
>>> assert used_gpu_i==expected
>>> assert used_gpu_g==expected

```

**forward**(*x\_dict*, *\*\*kwargs*)

**Parameters** *x\_dict* (*dict*) – Input variables.

**Returns**

- a tuple of `pixyz.losses.Loss` and `dict`
- *deterministically calculrated loss and updated all samples.*



### 3.1 Model

```
class pixyz.models.Model(loss,      test_loss=None,      distributions=[],      optimizer=<class
                        'torch.optim.adam.Adam'>,      optimizer_params={},
                        clip_grad_norm=None, clip_grad_value=None)
```

Bases: object

This class is for training and testing a loss class. It requires a defined loss class, distributions to train, and optimizer for initialization.

#### Examples

```
>>> import torch
>>> from torch import optim
>>> from torch.nn import functional as F
>>> from pixyz.distributions import Bernoulli, Normal
>>> from pixyz.losses import KullbackLeibler
...
>>> # Set distributions (Distribution API)
>>> class Inference(Normal):
...     def __init__(self):
...         super().__init__(var=["z"], cond_var=["x"], name="q")
...         self.model_loc = torch.nn.Linear(128, 64)
...         self.model_scale = torch.nn.Linear(128, 64)
...     def forward(self, x):
...         return {"loc": self.model_loc(x), "scale": F.softplus(self.model_
↪ scale(x))}
...
>>> class Generator(Bernoulli):
...     def __init__(self):
...         super().__init__(var=["x"], cond_var=["z"], name="p")
...         self.model = torch.nn.Linear(64, 128)
```

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```

...     def forward(self, z):
...         return {"probs": torch.sigmoid(self.model(z))}
...
>>> p = Generator()
>>> q = Inference()
>>> prior = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.),
...                 var=["z"], features_shape=[64], name="p_{prior}")
...
>>> # Define a loss function (Loss API)
>>> reconst = -p.log_prob().expectation(q)
>>> kl = KullbackLeibler(q,prior)
>>> loss_cls = (reconst - kl).mean()
>>> print(loss_cls)
mean \left(- D_{\text{KL}} \left[q(z|x) || p_{\text{prior}}(z) \right] - \mathbb{E}_{q(z|x)} \left[ \log p(x|z) \right] \right)
>>>
>>> # Set a model (Model API)
>>> model = Model(loss=loss_cls, distributions=[p, q],
...               optimizer=optim.Adam, optimizer_params={"lr": 1e-3})
>>> # Train and test the model
>>> data = torch.randn(1, 128) # Pseudo data
>>> train_loss = model.train({"x": data})
>>> test_loss = model.test({"x": data})

```

**\_\_init\_\_** (loss, test\_loss=None, distributions=[], optimizer=<class 'torch.optim.adam.Adam'>, optimizer\_params={}, clip\_grad\_norm=None, clip\_grad\_value=None)

#### Parameters

- **loss** (*pixyz.losses.Loss*) – Loss class for training.
- **test\_loss** (*pixyz.losses.Loss*) – Loss class for testing.
- **distributions** (*list*) – List of *pixyz.distributions.Distribution*.
- **optimizer** (*torch.optim*) – Optimization algorithm.
- **optimizer\_params** (*dict*) – Parameters of optimizer
- **clip\_grad\_norm** (*float or int*) – Maximum allowed norm of the gradients.
- **clip\_grad\_value** (*float or int*) – Maximum allowed value of the gradients.

**set\_loss** (loss, test\_loss=None)

**train** (train\_x\_dict={}, \*\*kwargs)

Train the model.

#### Parameters

- **train\_x\_dict** (*dict*) – Input data.
- **\*\*kwargs** –

**Returns** **loss** – Train loss value

**Return type** *torch.Tensor*

**test** (test\_x\_dict={}, \*\*kwargs)

Test the model.

#### Parameters

- **test\_x\_dict** (*dict*) – Input data

- **\*\*kwargs** –

**Returns** **loss** – Test loss value

**Return type** torch.Tensor

## 3.2 Pre-implementation models

### 3.2.1 ML

```
class pixyz.models.ML(p, other_distributions=[], optimizer=<class 'torch.optim.adam.Adam'>, optimizer_params={}, clip_grad_norm=False, clip_grad_value=False)
```

Bases: pixyz.models.model.Model

Maximum Likelihood (log-likelihood)

The negative log-likelihood of a given distribution (p) is set as the loss class of this model.

```
__init__(p, other_distributions=[], optimizer=<class 'torch.optim.adam.Adam'>, optimizer_params={}, clip_grad_norm=False, clip_grad_value=False)
```

#### Parameters

- **p** (*torch.distributions.Distribution*) – Classifier (distribution).
- **optimizer** (*torch.optim*) – Optimization algorithm.
- **optimizer\_params** (*dict*) – Parameters of optimizer
- **clip\_grad\_norm** (*float or int*) – Maximum allowed norm of the gradients.
- **clip\_grad\_value** (*float or int*) – Maximum allowed value of the gradients.

```
train(train_x_dict={}, **kwargs)
```

Train the model.

#### Parameters

- **train\_x\_dict** (*dict*) – Input data.
- **\*\*kwargs** –

**Returns** **loss** – Train loss value

**Return type** torch.Tensor

```
test(test_x_dict={}, **kwargs)
```

Test the model.

#### Parameters

- **test\_x\_dict** (*dict*) – Input data
- **\*\*kwargs** –

**Returns** **loss** – Test loss value

**Return type** torch.Tensor

### 3.2.2 VAE

```
class pixyz.models.VAE(encoder, decoder, other_distributions=[], regularizer=None, op-  
                      timizer=<class 'torch.optim.adam.Adam'>, optimizer_params={},  
                      clip_grad_norm=None, clip_grad_value=None)
```

Bases: `pixyz.models.model.Model`

Variational Autoencoder.

In VAE class, reconstruction loss on given distributions (encoder and decoder) is set as the default loss class. However, if you want to add additional terms, e.g., the KL divergence between encoder and prior, you need to set them to the *regularizer* argument, which defaults to `None`.

#### References

[Kingma+ 2013] Auto-Encoding Variational Bayes

```
__init__(encoder, decoder, other_distributions=[], regularizer=None, optimizer=<class  
         'torch.optim.adam.Adam'>, optimizer_params={}, clip_grad_norm=None,  
         clip_grad_value=None)
```

##### Parameters

- **encoder** (*torch.distributions.Distribution*) – Encoder distribution.
- **decoder** (*torch.distributions.Distribution*) – Decoder distribution.
- **regularizer** (*torch.losses.Loss, defaults to None*) – If you want to add additional terms to the loss, set them to this argument.
- **optimizer** (*torch.optim*) – Optimization algorithm.
- **optimizer\_params** (*dict*) – Parameters of optimizer
- **clip\_grad\_norm** (*float or int*) – Maximum allowed norm of the gradients.
- **clip\_grad\_value** (*float or int*) – Maximum allowed value of the gradients.

```
train(train_x_dict={}, **kwargs)
```

Train the model.

##### Parameters

- **train\_x\_dict** (*dict*) – Input data.
- **\*\*kwargs** –

**Returns** `loss` – Train loss value

**Return type** `torch.Tensor`

```
test(test_x_dict={}, **kwargs)
```

Test the model.

##### Parameters

- **test\_x\_dict** (*dict*) – Input data
- **\*\*kwargs** –

**Returns** `loss` – Test loss value

**Return type** `torch.Tensor`

### 3.2.3 VI

```
class pixyz.models.VI(p, approximate_dist, other_distributions=[], optimizer=<class
    'torch.optim.adam.Adam'>, optimizer_params={}, clip_grad_norm=None,
    clip_grad_value=None)
```

Bases: `pixyz.models.model.Model`

Variational Inference (Amortized inference)

The ELBO for given distributions (`p`, `approximate_dist`) is set as the loss class of this model.

```
__init__(p, approximate_dist, other_distributions=[], optimizer=<class 'torch.optim.adam.Adam'>,
    optimizer_params={}, clip_grad_norm=None, clip_grad_value=None)
```

#### Parameters

- **p** (`torch.distributions.Distribution`) – Generative model (distribution).
- **approximate\_dist** (`torch.distributions.Distribution`) – Approximate posterior distribution.
- **optimizer** (`torch.optim`) – Optimization algorithm.
- **optimizer\_params** (`dict`) – Parameters of optimizer
- **clip\_grad\_norm** (`float or int`) – Maximum allowed norm of the gradients.
- **clip\_grad\_value** (`float or int`) – Maximum allowed value of the gradients.

```
train(train_x_dict={}, **kwargs)
```

Train the model.

#### Parameters

- **train\_x\_dict** (`dict`) – Input data.
- **\*\*kwargs** –

**Returns** `loss` – Train loss value

**Return type** `torch.Tensor`

```
test(test_x_dict={}, **kwargs)
```

Test the model.

#### Parameters

- **test\_x\_dict** (`dict`) – Input data
- **\*\*kwargs** –

**Returns** `loss` – Test loss value

**Return type** `torch.Tensor`

### 3.2.4 GAN

```
class pixyz.models.GAN(p, discriminator, optimizer=<class 'torch.optim.adam.Adam'>, op-
    timizer_params={}, d_optimizer=<class 'torch.optim.adam.Adam'>,
    d_optimizer_params={}, clip_grad_norm=None, clip_grad_value=None)
```

Bases: `pixyz.models.model.Model`

Generative Adversarial Network

(Adversarial) Jensen-Shannon divergence between given distributions (`p_data`, `p`) is set as the loss class of this model.

## Examples

```

>>> import torch
>>> from torch import nn, optim
>>> from pixyz.distributions import Deterministic
>>> from pixyz.distributions import Normal
>>> from pixyz.models import GAN
>>> from pixyz.utils import print_latex
>>> x_dim = 128
>>> z_dim = 100
>>> ...
>>> # Set distributions (Distribution API)
>>> ...
>>> # generator model  $p(x|z)$ 
>>> class Generator(Deterministic):
...     def __init__(self):
...         super(Generator, self).__init__(var=["x"], cond_var=["z"], name="p")
...         self.model = nn.Sequential(
...             nn.Linear(z_dim, x_dim),
...             nn.Sigmoid()
...         )
...     def forward(self, z):
...         x = self.model(z)
...         return {"x": x}
>>> ...
>>> # prior model  $p(z)$ 
>>> prior = Normal(loc=torch.tensor(0.), scale=torch.tensor(1.),
...                 var=["z"], features_shape=[z_dim], name="p_{prior}")
>>> ...
>>> # generative model
>>> p_g = Generator()
>>> p = (p_g*prior).marginalize_var("z")
>>> ...
>>> # discriminator model  $p(t|x)$ 
>>> class Discriminator(Deterministic):
...     def __init__(self):
...         super(Discriminator, self).__init__(var=["t"], cond_var=["x"], name="d
↪")
...         self.model = nn.Sequential(
...             nn.Linear(x_dim, 1),
...             nn.Sigmoid()
...         )
...     def forward(self, x):
...         t = self.model(x)
...         return {"t": t}
>>> ...
>>> d = Discriminator()
>>> # Set a model (Model API)
>>> model = GAN(p, d, optimizer_params={"lr":0.0002}, d_optimizer_params={"lr":0.
↪0002})
>>> print(model)
Distributions (for training):
  p(x)
Loss function:
  mean(D_{JS}^{Adv} \left[p_{data}(x) || p(x) \right])
Optimizer:
  Adam (

```

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```

Parameter Group 0
  amsgrad: False
  betas: (0.9, 0.999)
  eps: 1e-08
  lr: 0.0002
  weight_decay: 0
)
>>> # Train and test the model
>>> data = torch.randn(1, x_dim) # Pseudo data
>>> train_loss = model.train({"x": data})
>>> test_loss = model.test({"x": data})

```

```

__init__(p, discriminator, optimizer=<class 'torch.optim.adam.Adam'>, optimizer_params={},
         d_optimizer=<class 'torch.optim.adam.Adam'>, d_optimizer_params={},
         clip_grad_norm=None, clip_grad_value=None)

```

**Parameters**

- **p** (*torch.distributions.Distribution*) – Generative model (generator).
- **discriminator** (*torch.distributions.Distribution*) – Critic (discriminator).
- **optimizer** (*torch.optim*) – Optimization algorithm.
- **optimizer\_params** (*dict*) – Parameters of optimizer
- **clip\_grad\_norm** (*float or int*) – Maximum allowed norm of the gradients.
- **clip\_grad\_value** (*float or int*) – Maximum allowed value of the gradients.

```
train(train_x_dict={}, adversarial_loss=True, **kwargs)
```

Train the model.

**Parameters**

- **train\_x\_dict** (*dict, defaults to {}*) – Input data.
- **adversarial\_loss** (*bool, defaults to True*) – Whether to train the discriminator.
- **\*\*kwargs** –

**Returns**

- **loss** (*torch.Tensor*) – Train loss value.
- **d\_loss** (*torch.Tensor*) – Train loss value of the discriminator (if `adversarial_loss` is `True`).

```
test(test_x_dict={}, adversarial_loss=True, **kwargs)
```

Train the model.

**Parameters**

- **test\_x\_dict** (*dict, defaults to {}*) – Input data.
- **adversarial\_loss** (*bool, defaults to True*) – Whether to return the discriminator loss.
- **\*\*kwargs** –

**Returns**

- **loss** (*torch.Tensor*) – Test loss value.

- **d\_loss** (*torch.Tensor*) – Test loss value of the discriminator (if `adversarial_loss` is `True`).

## 4.1 Flow

**class** pixyz.flows.**Flow**(*in\_features*)

Bases: torch.nn.modules.module.Module

Flow class. In Pixyz, all flows are required to inherit this class.

**\_\_init\_\_**(*in\_features*)

**Parameters** *in\_features* (*int*) – Size of input data.

**in\_features**

**forward**(*x*, *y=None*, *compute\_jacobian=True*)

Forward propagation of flow layers.

**Parameters**

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, *defaults to None*) – Data for conditioning.
- **compute\_jacobian** (*bool*, *defaults to True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in *logdet\_jacobian*.

**Returns** *z*

**Return type** torch.Tensor

**inverse**(*z*, *y=None*)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

**Parameters**

- **z** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, *defaults to None*) – Data for conditioning.

**Returns** `x`

**Return type** `torch.Tensor`

**logdet\_jacobian**

Get log-determinant Jacobian.

Before calling this, you should run `forward` or `update_jacobian` methods to calculate and store log-determinant Jacobian.

**class** `pixyz.flows.FlowList` (*flow\_list*)

Bases: `pixyz.flows.flows.Flow`

**\_\_init\_\_** (*flow\_list*)

Hold flow modules in a list.

Once initializing, it can be handled as a single flow module.

## Notes

Indexing is not supported for now.

**Parameters** `flow_list` (*list*) –

**forward** (*x*, *y=None*, *compute\_jacobian=True*)

Forward propagation of flow layers.

**Parameters**

- `x` (*torch.Tensor*) – Input data.
- `y` (*torch.Tensor*, *defaults to None*) – Data for conditioning.
- `compute_jacobian` (*bool*, *defaults to True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in `logdet_jacobian`.

**Returns** `z`

**Return type** `torch.Tensor`

**inverse** (*z*, *y=None*)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

**Parameters**

- `z` (*torch.Tensor*) – Input data.
- `y` (*torch.Tensor*, *defaults to None*) – Data for conditioning.

**Returns** `x`

**Return type** `torch.Tensor`

## 4.2 Normalizing flow

### 4.2.1 PlanarFlow

**class** `pixyz.flows.PlanarFlow` (*in\_features*, *constraint\_u=False*)

Bases: `pixyz.flows.flows.Flow`

Planar flow.

$$f(\mathbf{x}) = \mathbf{x} + \mathbf{u}h(\mathbf{w}^T \mathbf{x} + \mathbf{b})$$

**deriv\_tanh** (*x*)

**reset\_parameters** ()

**forward** (*x*, *y=None*, *compute\_jacobian=True*)

Forward propagation of flow layers.

**Parameters**

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, *defaults to None*) – Data for conditioning.
- **compute\_jacobian** (*bool*, *defaults to True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in `logdet_jacobian`.

**Returns z**

**Return type** `torch.Tensor`

**inverse** (*z*, *y=None*)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

**Parameters**

- **z** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, *defaults to None*) – Data for conditioning.

**Returns x**

**Return type** `torch.Tensor`

**extra\_repr** ()

Set the extra representation of the module

To print customized extra information, you should re-implement this method in your own modules. Both single-line and multi-line strings are acceptable.

## 4.3 Coupling layer

### 4.3.1 AffineCoupling

```
class pixyz.flows.AffineCoupling(in_features, mask_type='channel_wise', scale_net=None,  
                                translate_net=None, scale_translate_net=None, inverse_mask=False)
```

Bases: `pixyz.flows.flows.Flow`

Affine coupling layer

$$\begin{aligned} \mathbf{y}_{1:d} &= \mathbf{x}_{1:d} \\ \mathbf{y}_{d+1:D} &= \mathbf{x}_{d+1:D} \odot \exp(s(\mathbf{x}_{1:d}) + t(\mathbf{x}_{1:d})) \end{aligned}$$

**build\_mask** (*x*)

**Parameters** *x* (*torch.Tensor*) –

**Returns** *mask*

**Return type** *torch.tensor*

### Examples

```
>>> scale_translate_net = lambda x: (x, x)
>>> f1 = AffineCoupling(4, mask_type="channel_wise", scale_translate_
↳ net=scale_translate_net,
...                               inverse_mask=False)
>>> x1 = torch.randn([1,4,3,3])
>>> f1.build_mask(x1)
tensor([[[[1.]],
<BLANKLINE>
          [[1.]],
<BLANKLINE>
          [[0.]],
<BLANKLINE>
          [[0.]]]])
>>> f2 = AffineCoupling(2, mask_type="checkerboard", scale_translate_
↳ net=scale_translate_net,
...                               inverse_mask=True)
>>> x2 = torch.randn([1,2,5,5])
>>> f2.build_mask(x2)
tensor([[[[0., 1., 0., 1., 0.],
          [1., 0., 1., 0., 1.],
          [0., 1., 0., 1., 0.],
          [1., 0., 1., 0., 1.],
          [0., 1., 0., 1., 0.]]]])
```

**get\_parameters** (*x*, *y=None*)

**Parameters**

- *x* (*torch.tensor*) –
- *y* (*torch.tensor*) –

**Returns**

- *s* (*torch.tensor*)
- *t* (*torch.tensor*)

### Examples

```
>>> # In case of using scale_translate_net
>>> scale_translate_net = lambda x: (x, x)
>>> f1 = AffineCoupling(4, mask_type="channel_wise", scale_translate_
↳ net=scale_translate_net,
...                               inverse_mask=False)
>>> x1 = torch.randn([1,4,3,3])
>>> log_s, t = f1.get_parameters(x1)
>>> # In case of using scale_net and translate_net
```

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```

>>> scale_net = lambda x: x
>>> translate_net = lambda x: x
>>> f2 = AffineCoupling(4, mask_type="channel_wise", scale_net=scale_net,
↳ translate_net=translate_net,
...                          inverse_mask=False)
>>> x2 = torch.randn([1,4,3,3])
>>> log_s, t = f2.get_parameters(x2)

```

**forward** (*x*, *y=None*, *compute\_jacobian=True*)

Forward propagation of flow layers.

#### Parameters

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.
- **compute\_jacobian** (*bool*, defaults to *True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in `logdet_jacobian`.

#### Returns z

**Return type** *torch.Tensor*

**inverse** (*z*, *y=None*)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

#### Parameters

- **z** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.

#### Returns x

**Return type** *torch.Tensor*

**extra\_repr** ()

Set the extra representation of the module

To print customized extra information, you should re-implement this method in your own modules. Both single-line and multi-line strings are acceptable.

## 4.4 Invertible layer

### 4.4.1 ChannelConv

**class** `pixyz.flows.ChannelConv` (*in\_channels*, *decomposed=False*)

Bases: `pixyz.flows.flows.Flow`

Invertible  $1 \times 1$  convolution.

#### Notes

This is implemented with reference to the following code. <https://github.com/chaiyujin/flow-pytorch/blob/master/flow/modules.py>

**get\_parameters** (*x*, *inverse*)

**forward** (*x*, *y=None*, *compute\_jacobian=True*)

Forward propagation of flow layers.

**Parameters**

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, *defaults to None*) – Data for conditioning.
- **compute\_jacobian** (*bool*, *defaults to True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in `logdet_jacobian`.

**Returns** *z*

**Return type** *torch.Tensor*

**inverse** (*x*, *y=None*)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

**Parameters**

- **z** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, *defaults to None*) – Data for conditioning.

**Returns** *x*

**Return type** *torch.Tensor*

## 4.5 Operation layer

### 4.5.1 Squeeze

**class** `pixyz.flows.Squeeze`

Bases: `pixyz.flows.flows.Flow`

Squeeze operation.

$c * s * s \rightarrow 4c * s/2 * s/2$

**Examples**

```
>>> import torch
>>> a = torch.tensor([i+1 for i in range(16)]).view(1,1,4,4)
>>> print(a)
tensor([[[[ 1,  2,  3,  4],
           [ 5,  6,  7,  8],
           [ 9, 10, 11, 12],
           [13, 14, 15, 16]]]])
>>> f = Squeeze()
>>> print(f(a))
tensor([[[[ 1,  3],
           [ 9, 11]],
<BLANKLINE>
          [[ 2,  4],
           [10, 12]],
<BLANKLINE>
```

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```

        [[ 5,  7],
         [13, 15]],
<BLANKLINE>
        [[ 6,  8],
         [14, 16]]]])

```

```

>>> print(f.inverse(f(a)))
tensor([[[[ 1,  2,  3,  4],
           [ 5,  6,  7,  8],
           [ 9, 10, 11, 12],
           [13, 14, 15, 16]]]])

```

**forward** (*x*, *y=None*, *compute\_jacobian=True*)

Forward propagation of flow layers.

#### Parameters

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.
- **compute\_jacobian** (*bool*, defaults to *True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in *logdet\_jacobian*.

#### Returns z

**Return type** *torch.Tensor*

**inverse** (*z*, *y=None*)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

#### Parameters

- **z** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.

#### Returns x

**Return type** *torch.Tensor*

## 4.5.2 Unsqueeze

**class** *pixyz.flows.Unsqueeze*

Bases: *pixyz.flows.operations.Squeeze*

Unsqueeze operation.

$c * s * s \rightarrow c/4 * 2s * 2s$

#### Examples

```

>>> import torch
>>> a = torch.tensor([i+1 for i in range(16)]).view(1,4,2,2)
>>> print(a)
tensor([[[[ 1,  2],
           [ 3,  4]],

```

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```

<BLANKLINE>
        [[ 5,  6],
         [ 7,  8]],
<BLANKLINE>
        [[ 9, 10],
         [11, 12]],
<BLANKLINE>
        [[13, 14],
         [15, 16]]]])
>>> f = Unsqueeze()
>>> print(f(a))
tensor([[[[ 1,  5,  2,  6],
           [ 9, 13, 10, 14],
           [ 3,  7,  4,  8],
           [11, 15, 12, 16]]]])
>>> print(f.inverse(f(a)))
tensor([[[[ 1,  2],
           [ 3,  4]],
<BLANKLINE>
        [[ 5,  6],
         [ 7,  8]],
<BLANKLINE>
        [[ 9, 10],
         [11, 12]],
<BLANKLINE>
        [[13, 14],
         [15, 16]]]])

```

**forward** (*x*, *y=None*, *compute\_jacobian=True*)

Forward propagation of flow layers.

#### Parameters

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.
- **compute\_jacobian** (*bool*, defaults to *True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in *logdet\_jacobian*.

#### Returns z

**Return type** *torch.Tensor*

**inverse** (*z*, *y=None*)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

#### Parameters

- **z** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.

#### Returns x

**Return type** *torch.Tensor*

### 4.5.3 Permutation

**class** pixyz.flows.**Permutation** (*permute\_indices*)  
 Bases: pixyz.flows.flows.Flow

#### Examples

```
>>> import torch
>>> a = torch.tensor([i+1 for i in range(16)]).view(1,4,2,2)
>>> print(a)
tensor([[[[ 1,  2],
           [ 3,  4]],
         <BLANKLINE>
          [[ 5,  6],
           [ 7,  8]],
         <BLANKLINE>
          [[ 9, 10],
           [11, 12]],
         <BLANKLINE>
          [[13, 14],
           [15, 16]]]])
>>> perm = [0,3,1,2]
>>> f = Permutation(perm)
>>> f(a)
tensor([[[[ 1,  2],
           [ 3,  4]],
         <BLANKLINE>
          [[13, 14],
           [15, 16]],
         <BLANKLINE>
          [[ 5,  6],
           [ 7,  8]],
         <BLANKLINE>
          [[ 9, 10],
           [11, 12]]]])
>>> f.inverse(f(a))
tensor([[[[ 1,  2],
           [ 3,  4]],
         <BLANKLINE>
          [[ 5,  6],
           [ 7,  8]],
         <BLANKLINE>
          [[ 9, 10],
           [11, 12]],
         <BLANKLINE>
          [[13, 14],
           [15, 16]]]])
```

**forward** (*x*, *y=None*, *compute\_jacobian=True*)  
 Forward propagation of flow layers.

#### Parameters

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor*, defaults to *None*) – Data for conditioning.
- **compute\_jacobian** (*bool*, defaults to *True*) – Whether to calculate and

store log-determinant Jacobian. If true, calculated Jacobian values are stored in `logdet_jacobian`.

**Returns** `z`

**Return type** `torch.Tensor`

**inverse** (`z`, `y=None`)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

**Parameters**

- `z` (`torch.Tensor`) – Input data.
- `y` (`torch.Tensor`, defaults to `None`) – Data for conditioning.

**Returns** `x`

**Return type** `torch.Tensor`

#### 4.5.4 Shuffle

**class** `pixyz.flows.Shuffle` (`in_features`)

Bases: `pixyz.flows.operations.Permutation`

#### 4.5.5 Reverse

**class** `pixyz.flows.Reverse` (`in_features`)

Bases: `pixyz.flows.operations.Permutation`

#### 4.5.6 Flatten

**class** `pixyz.flows.Flatten` (`in_size=None`)

Bases: `pixyz.flows.flows.Flow`

**forward** (`x`, `y=None`, `compute_jacobian=True`)

Forward propagation of flow layers.

**Parameters**

- `x` (`torch.Tensor`) – Input data.
- `y` (`torch.Tensor`, defaults to `None`) – Data for conditioning.
- `compute_jacobian` (`bool`, defaults to `True`) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in `logdet_jacobian`.

**Returns** `z`

**Return type** `torch.Tensor`

**inverse** (`z`, `y=None`)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

**Parameters**

- `z` (`torch.Tensor`) – Input data.
- `y` (`torch.Tensor`, defaults to `None`) – Data for conditioning.

**Returns** `x`

**Return type** `torch.Tensor`

### 4.5.7 BatchNorm1d

**class** `pixyz.flows.BatchNorm1d(in_features, momentum=0.0)`

Bases: `pixyz.flows.flows.Flow`

A batch normalization with the inverse transformation.

#### Notes

This is implemented with reference to the following code. <https://github.com/ikostrikov/pytorch-flows/blob/master/flows.py#L205>

#### Examples

```
>>> x = torch.randn(20, 100)
>>> f = BatchNorm1d(100)
>>> # transformation
>>> z = f(x)
>>> # reconstruction
>>> _x = f.inverse(f(x))
>>> # check this reconstruction
>>> diff = torch.sum(torch.abs(_x-x)).item()
>>> diff < 0.1
True
```

**forward** (`x`, `y=None`, `compute_jacobian=True`)

Forward propagation of flow layers.

#### Parameters

- `x` (`torch.Tensor`) – Input data.
- `y` (`torch.Tensor`, defaults to `None`) – Data for conditioning.
- `compute_jacobian` (`bool`, defaults to `True`) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in `logdet_jacobian`.

**Returns** `z`

**Return type** `torch.Tensor`

**inverse** (`z`, `y=None`)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

#### Parameters

- `z` (`torch.Tensor`) – Input data.
- `y` (`torch.Tensor`, defaults to `None`) – Data for conditioning.

**Returns** `x`

**Return type** `torch.Tensor`

### 4.5.8 BatchNorm2d

**class** pixyz.flows.**BatchNorm2d**(*in\_features, momentum=0.0*)

Bases: pixyz.flows.normalizations.BatchNorm1d

A batch normalization with the inverse transformation.

#### Notes

This is implemented with reference to the following code. <https://github.com/ikostrikov/pytorch-flows/blob/master/flows.py#L205>

#### Examples

```
>>> x = torch.randn(20, 100, 35, 45)
>>> f = BatchNorm2d(100)
>>> # transformation
>>> z = f(x)
>>> # reconstruction
>>> _x = f.inverse(f(x))
>>> # check this reconstruction
>>> diff = torch.sum(torch.abs(_x-x)).item()
>>> diff < 0.1
True
```

### 4.5.9 ActNorm2d

**class** pixyz.flows.**ActNorm2d**(*in\_features, scale=1.0*)

Bases: pixyz.flows.flows.Flow

Activation Normalization Initialize the bias and scale with a given minibatch, so that the output per-channel have zero mean and unit variance for that. After initialization, *bias* and *logs* will be trained as parameters.

#### Notes

This is implemented with reference to the following code. <https://github.com/chaiyujin/glow-pytorch/blob/master/glow/modules.py>

**initialize\_parameters**(*x*)

**forward**(*x, y=None, compute\_jacobian=True*)

Forward propagation of flow layers.

#### Parameters

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor, defaults to None*) – Data for conditioning.
- **compute\_jacobian** (*bool, defaults to True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in `logdet_jacobian`.

#### Returns **z**

**Return type** torch.Tensor

**inverse** (*x*, *y=None*)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

**Parameters**

- **z** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor, defaults to None*) – Data for conditioning.

**Returns** **x**

**Return type** *torch.Tensor*

## 4.5.10 Preprocess

**class** *pixyz.flows.Preprocess*

Bases: *pixyz.flows.flows.Flow*

**static logit** (*x*)

**forward** (*x*, *y=None*, *compute\_jacobian=True*)

Forward propagation of flow layers.

**Parameters**

- **x** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor, defaults to None*) – Data for conditioning.
- **compute\_jacobian** (*bool, defaults to True*) – Whether to calculate and store log-determinant Jacobian. If true, calculated Jacobian values are stored in *logdet\_jacobian*.

**Returns** **z**

**Return type** *torch.Tensor*

**inverse** (*z*, *y=None*)

Backward (inverse) propagation of flow layers. In this method, log-determinant Jacobian is not calculated.

**Parameters**

- **z** (*torch.Tensor*) – Input data.
- **y** (*torch.Tensor, defaults to None*) – Data for conditioning.

**Returns** **x**

**Return type** *torch.Tensor*





`pixyz.utils.set_epsilon(eps)`

Set a *epsilon* parameter.

**Parameters** *eps* (*int* or *float*)–

### Examples

```
>>> from unittest import mock
>>> with mock.patch('pixyz.utils._EPSILON', 1e-07):
...     set_epsilon(1e-06)
...     epsilon()
1e-06
```

`pixyz.utils.epsilon()`

Get a *epsilon* parameter.

**Returns**

**Return type** *int* or *float*

### Examples

```
>>> from unittest import mock
>>> with mock.patch('pixyz.utils._EPSILON', 1e-07):
...     epsilon()
1e-07
```

`pixyz.utils.get_dict_values(dicts, keys, return_dict=False)`

Get values from *dicts* specified by *keys*.

When *return\_dict* is *True*, return values are in dictionary format.

**Parameters**

- **dicts** (*dict*) –
- **keys** (*list*) –
- **return\_dict** (*bool*) –

**Returns**

**Return type** dict or list

### Examples

```
>>> get_dict_values({"a":1, "b":2, "c":3}, ["b"])
[2]
>>> get_dict_values({"a":1, "b":2, "c":3}, ["b", "d"], True)
{'b': 2}
```

`pixyz.utils.delete_dict_values` (*dicts*, *keys*)

Delete values from *dicts* specified by *keys*.

**Parameters**

- **dicts** (*dict*) –
- **keys** (*list*) –

**Returns** *new\_dicts*

**Return type** dict

### Examples

```
>>> delete_dict_values({"a":1, "b":2, "c":3}, ["b", "d"])
{'a': 1, 'c': 3}
```

`pixyz.utils.detach_dict` (*dicts*)

Detach all values in *dicts*.

**Parameters** **dicts** (*dict*) –

**Returns**

**Return type** dict

`pixyz.utils.replace_dict_keys` (*dicts*, *replace\_list\_dict*)

Replace values in *dicts* according to *replace\_list\_dict*.

**Parameters**

- **dicts** (*dict*) – Dictionary.
- **replace\_list\_dict** (*dict*) – Dictionary.

**Returns** *replaced\_dicts* – Dictionary.

**Return type** dict

## Examples

```
>>> replace_dict_keys({"a":1,"b":2,"c":3}, {"a":"x","b":"y"})
{'x': 1, 'y': 2, 'c': 3}
>>> replace_dict_keys({"a":1,"b":2,"c":3}, {"a":"x","e":"y"}) # keys of `replace_
↪list_dict`
{'x': 1, 'b': 2, 'c': 3}
```

`pixyz.utils.replace_dict_keys_split(dict, replace_list_dict)`  
 Replace values in *dicts* according to *replace\_list\_dict*.

Replaced dict is splitted by *replaced\_dict* and *remain\_dict*.

### Parameters

- **dicts** (*dict*) – Dictionary.
- **replace\_list\_dict** (*dict*) – Dictionary.

### Returns

- **replaced\_dict** (*dict*) – Dictionary.
- **remain\_dict** (*dict*) – Dictionary.

## Examples

```
>>> replace_list_dict = {'a': 'loc'}
>>> x_dict = {'a': 0, 'b': 1}
>>> print(replace_dict_keys_split(x_dict, replace_list_dict))
({'loc': 0}, {'b': 1})
```

**class** `pixyz.utils.FrozenSampleDict(dict_)`  
 Bases: `object`

`pixyz.utils.lru_cache_for_sample_dict(maxsize=0)`

Memoize the calculation result linked to the argument of sample dict. Note that dictionary arguments of the target function must be sample dict.

**Parameters** *maxsize* (cache size prepared for the target method) –

### Returns

**Return type** decorator function

## Examples

```
>>> import time
>>> import torch.nn as nn
>>> import pixyz.utils as utils
>>> # utils.CACHE_SIZE = 2 # you can also use this module option to enable all_
↪memoization of distribution
>>> import pixyz.distributions as pd
>>> class LongEncoder(pd.Normal):
...     def __init__(self):
...         super().__init__(var=['x'], cond_var=['y'])
...         self.nn = nn.Sequential(*(nn.Linear(1,1) for i in range(10000)))
...     def forward(self, y):
```

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```

...         return {'loc': self.nn(y), 'scale': torch.ones(1,1)}
...     @lru_cache_for_sample_dict(maxsize=2)
...     def get_params(self, params_dict={}, **kwargs):
...         return super().get_params(params_dict, **kwargs)
>>> def measure_time(func):
...     start = time.time()
...     func()
...     elapsed_time = time.time() - start
...     return elapsed_time
>>> le = LongEncoder()
>>> y = torch.ones(1, 1)
>>> t_sample1 = measure_time(lambda:le.sample({'y': y}))
>>> print ("sample1:{0}".format(t_sample1) + "[sec]") # doctest: +SKIP
>>> t_log_prob = measure_time(lambda:le.get_log_prob({'x': y, 'y': y}))
>>> print ("log_prob:{0}".format(t_log_prob) + "[sec]") # doctest: +SKIP
>>> t_sample2 = measure_time(lambda:le.sample({'y': y}))
>>> print ("sample2:{0}".format(t_sample2) + "[sec]") # doctest: +SKIP
>>> assert t_sample1 > t_sample2, "processing time increases: {0}".format(t_
↪sample2 - t_sample1)

```

`pixyz.utils.tolist(a)`

Convert a given input to the dictionary format.

**Parameters** *a* (list or other)–

**Returns**

**Return type** list

### Examples

```

>>> tolist(2)
[2]
>>> tolist([1, 2])
[1, 2]
>>> tolist([])
[]

```

`pixyz.utils.sum_samples(samples)`

Sum a given sample across the axes.

**Parameters** *samples* (*torch.Tensor*) – Input sample. The number of this axes is assumed to be 4 or less.

**Returns** Sum over all axes except the first axis.

**Return type** *torch.Tensor*

### Examples

```

>>> a = torch.ones([2])
>>> sum_samples(a).size()
torch.Size([2])
>>> a = torch.ones([2, 3])
>>> sum_samples(a).size()

```

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```
torch.Size([2])
>>> a = torch.ones([2, 3, 4])
>>> sum_samples(a).size()
torch.Size([2])
```

`pixyz.utils.print_latex(obj)`

Print formulas in latex format.

**Parameters** `obj` (`pixyz.distributions.distributions.Distribution`,  
`pixyz.losses.losses.Loss` or `pixyz.models.model.Model`.) –

`pixyz.utils.convert_latex_name(name)`



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